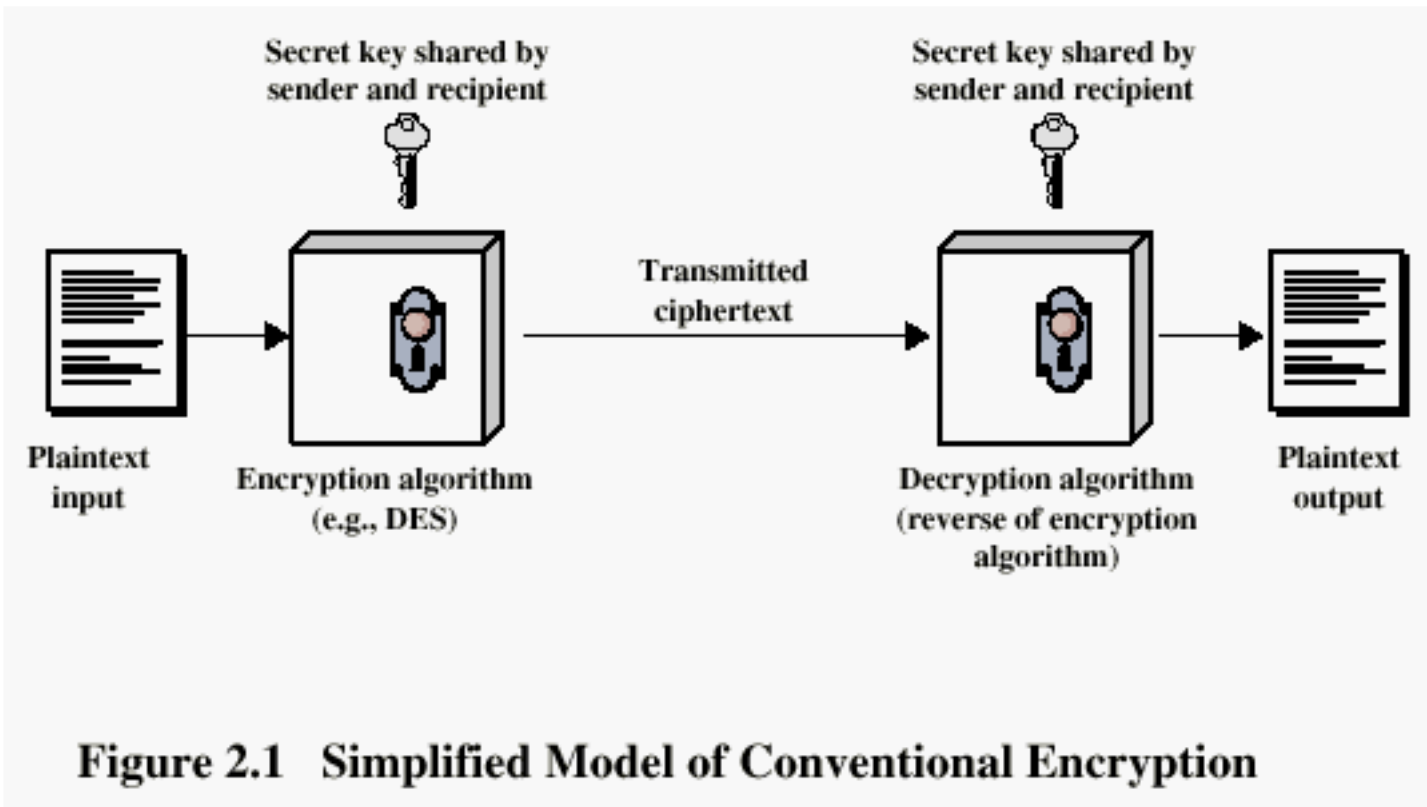


# Conventional Encryption Principles

- An encryption scheme has five ingredients:
  - Plaintext
  - Encryption algorithm
  - Secret Key
  - Ciphertext
  - Decryption algorithm
- Security depends on the secrecy of the key, not the secrecy of the algorithm

# Conventional Encryption Principles



# The 3 CRYPTs

- **Cryptology**= Cryptography + Cryptanalysis
- **Cryptography**= Deals with design of algorithms for encryption and decryption, intended to ensure the secrecy and/or authenticity of messages.
- **Cryptanalysis**= Deals with breaking of a cipher (algorithm) to recover information, or forging encrypted information that will be accepted as authentic.

# Cryptography

- Classified along three independent dimensions:
  1. The type of operations used for transforming plaintext to ciphertext
  2. The number of keys used
    - a) symmetric (single key)
    - b) asymmetric (two-keys, or public-key encryption)
  3. The way in which the plaintext is processed



German Lorenz cipher machine, used in World War II to encrypt very-high-level general staff messages

# Cryptanalysis

- The process of attempting to discover the plaintext or key is known as cryptanalysis.
- The strategy used by the cryptanalyst depends on nature of the encryption scheme and the information available to the cryptanalyst.

**Table 2.1 Types of Attacks on Encrypted Messages**

| Type of Attack    | Known to Cryptanalyst                                                                                                                                                                                                                                                                                                                                                       |
|-------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Ciphertext only   | <ul style="list-style-type: none"><li>•Encryption algorithm</li><li>•Ciphertext to be decoded</li></ul>                                                                                                                                                                                                                                                                     |
| Known plaintext   | <ul style="list-style-type: none"><li>•Encryption algorithm</li><li>•Ciphertext to be decoded</li><li>•One or more plaintext-ciphertext pairs formed with the secret key</li></ul>                                                                                                                                                                                          |
| Chosen plaintext  | <ul style="list-style-type: none"><li>•Encryption algorithm</li><li>•Ciphertext to be decoded</li><li>•Plaintext message chosen by cryptanalyst, together with its corresponding ciphertext generated with the secret key</li></ul>                                                                                                                                         |
| Chosen ciphertext | <ul style="list-style-type: none"><li>•Encryption algorithm</li><li>•Ciphertext to be decoded</li><li>•Purported ciphertext chosen by cryptanalyst, together with its corresponding decrypted plaintext generated with the secret key</li></ul>                                                                                                                             |
| Chosen text       | <ul style="list-style-type: none"><li>•Encryption algorithm</li><li>•Ciphertext to be decoded</li><li>•Plaintext message chosen by cryptanalyst, together with its corresponding ciphertext generated with the secret key</li><li>•Purported ciphertext chosen by cryptanalyst, together with its corresponding decrypted plaintext generated with the secret key</li></ul> |

# Average time required for exhaustive key search

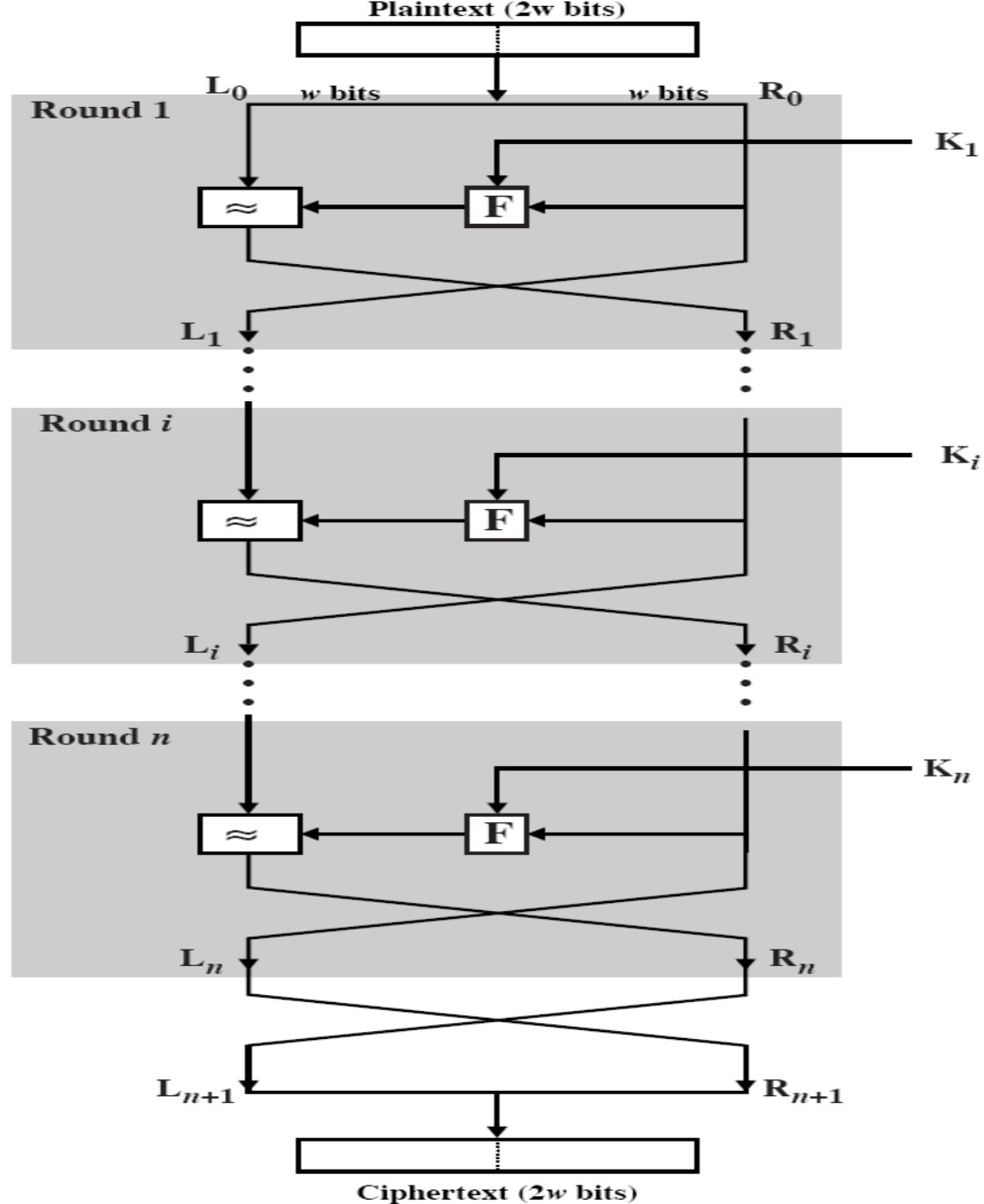
| Key Size (bits) | Number of Alternative Keys     | Time required at $10^6$ Decryption/ $\mu s$ |
|-----------------|--------------------------------|---------------------------------------------|
| 32              | $2^{32} = 4.3 \times 10^9$     | 2.15 milliseconds                           |
| 56              | $2^{56} = 7.2 \times 10^{16}$  | 10 hours                                    |
| 128             | $2^{128} = 3.4 \times 10^{38}$ | $5.4 \times 10^{18}$ years                  |
| 168             | $2^{168} = 3.7 \times 10^{50}$ | $5.9 \times 10^{30}$ years                  |

# Feistel Cipher Structure

- Virtually all conventional block encryption algorithms, including DES have a structure first described by Horst Feistel of IBM in 1973
- The realization of a Feistel Network depends on the choice of the following parameters and design features (see next slide):

# Feistel Cipher Structure

- **Block size:** larger block sizes mean greater security
- **Key Size:** larger key size means greater security
- **Number of rounds:** multiple rounds offer increasing security
- **Subkey generation algorithm:** greater complexity will lead to greater difficulty of cryptanalysis.
- **Fast software encryption/decryption:** the speed of execution of the algorithm becomes a concern



**Figure 3.5 Classical Feistel Network**

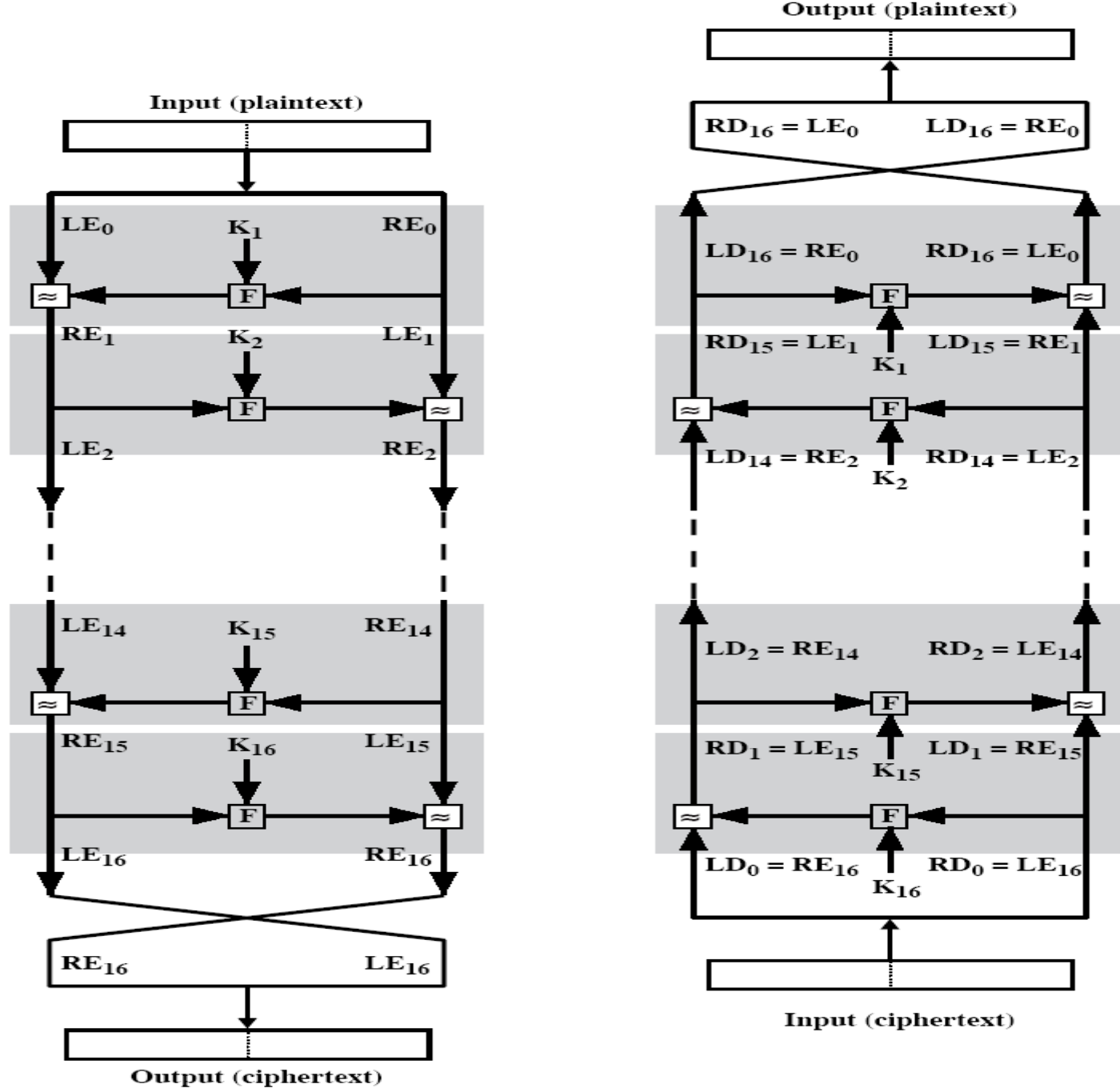


Figure 3.6 Feistel Encryption and Decryption

# Simplified DES(S-DES)

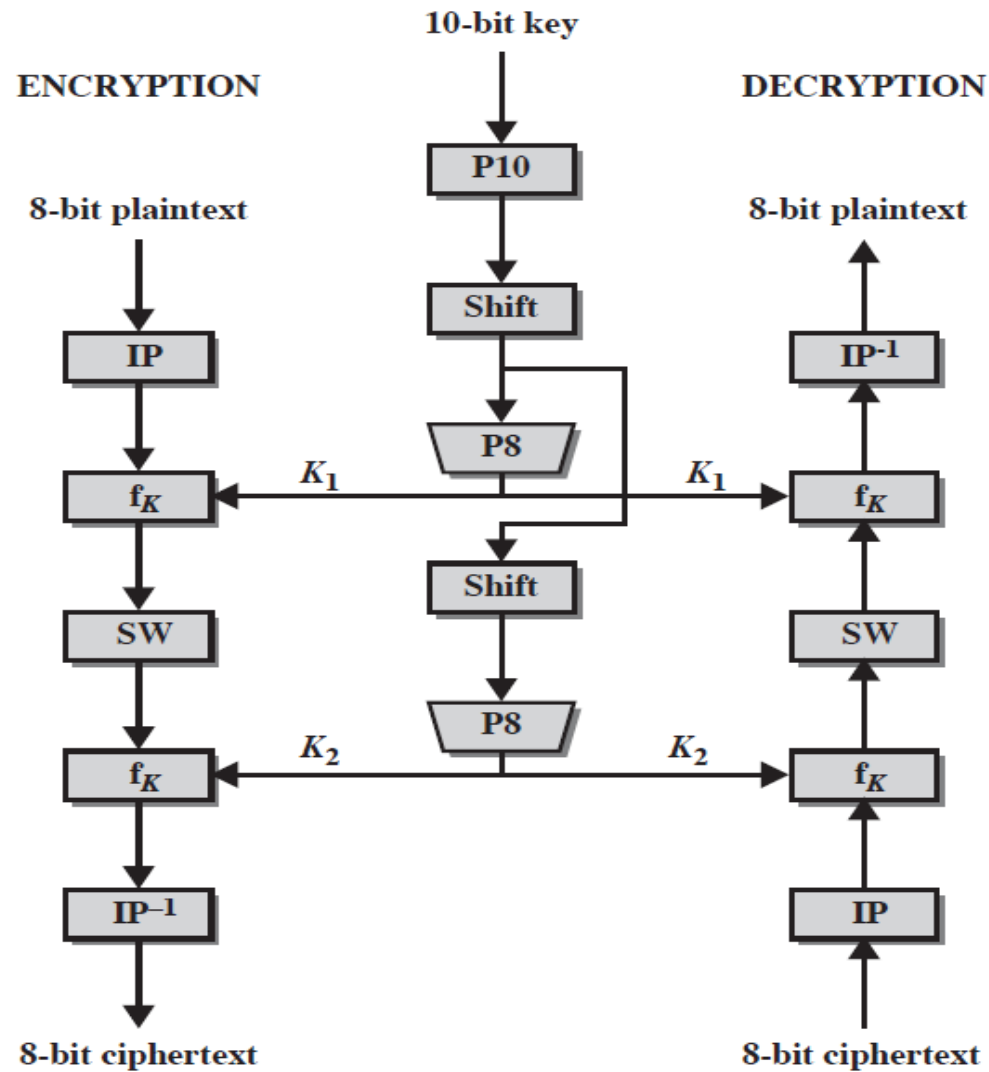
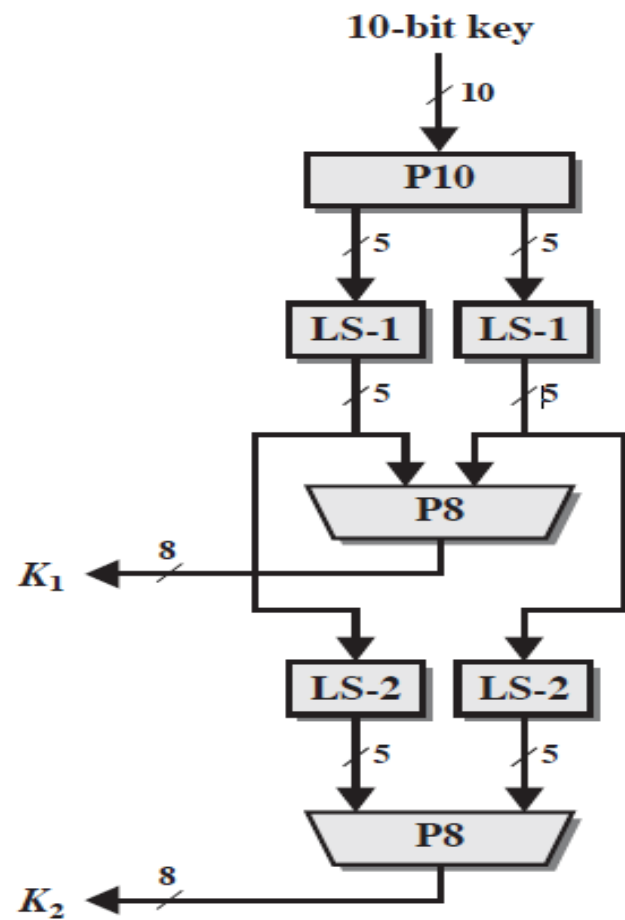
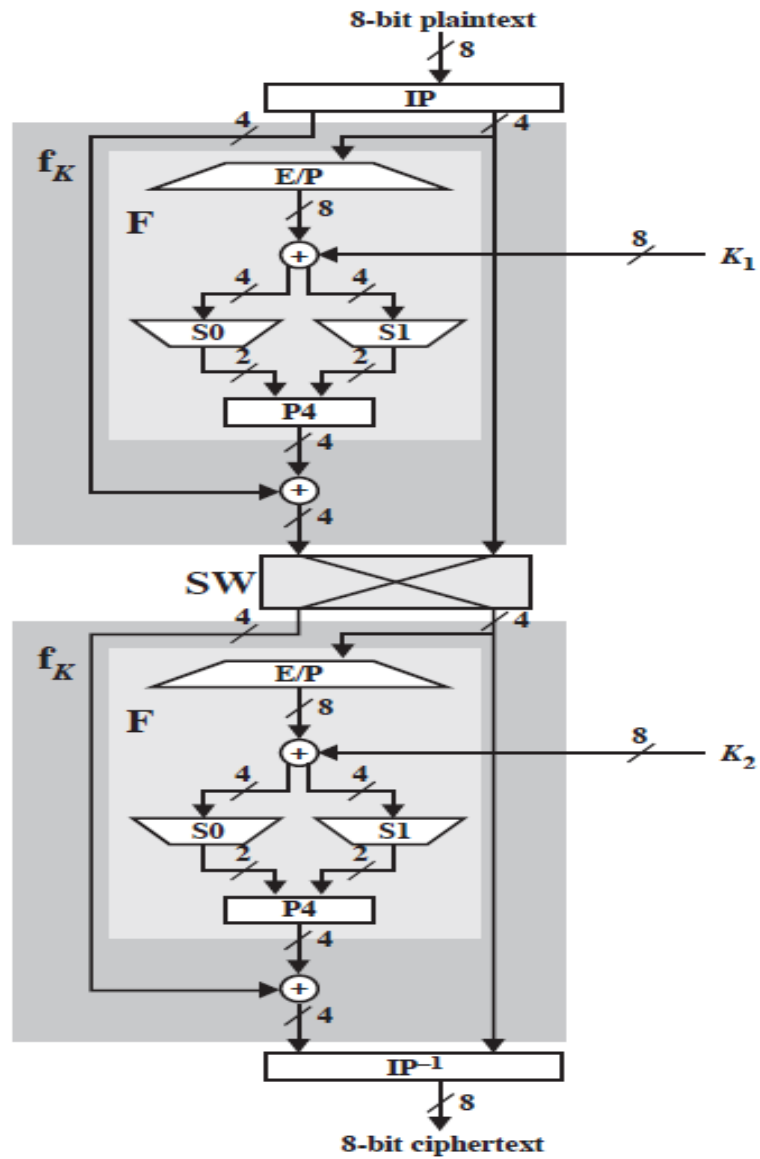


Figure G.1 Simplified DES Scheme



**Figure G.2** Key Generation for Simplified DES

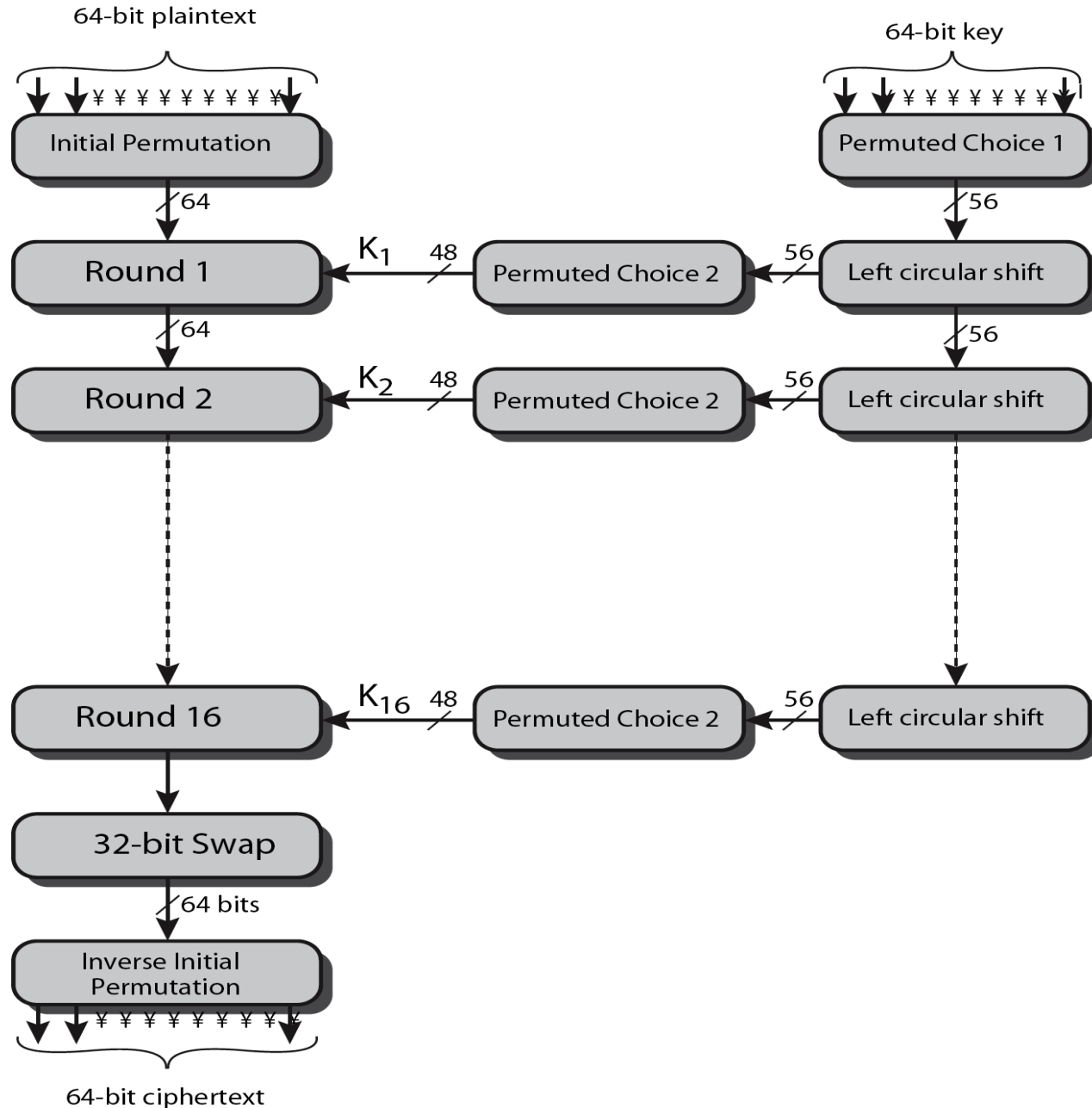


**Figure G.3 Simplified DES Encryption Detail**

# Conventional Encryption Algorithms

- Data Encryption Standard (DES)
  - The most widely used encryption scheme
  - The algorithm is referred to the Data Encryption Algorithm (DEA)
  - DES is a block cipher
  - The plaintext is processed in 64-bit blocks
  - The key is 56-bits in length

# DES Encryption Overview



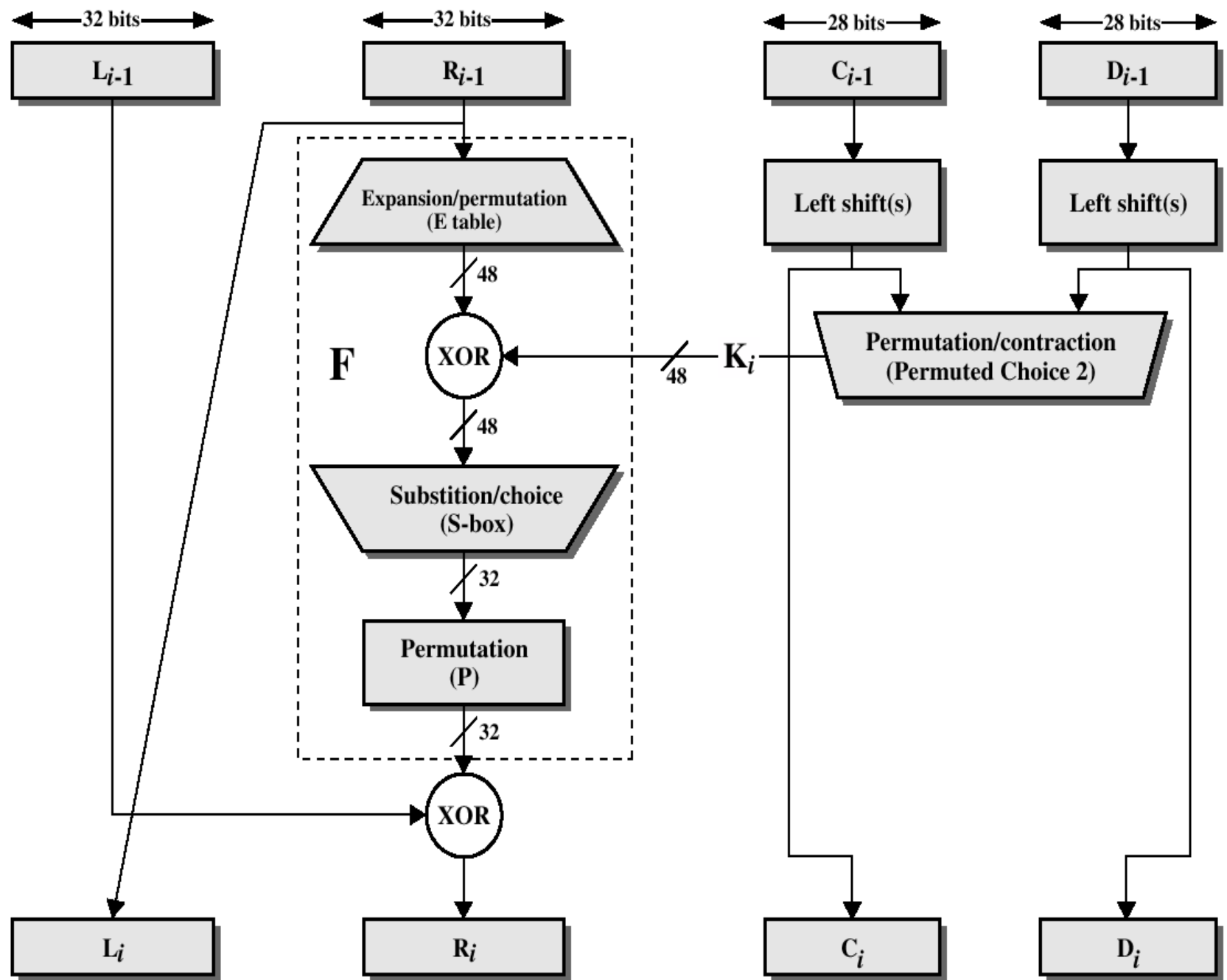


Figure 2.4 Single Round of DES Algorithm

# DES Round Structure

- uses two 32-bit L & R halves
- as for any Feistel cipher can describe as:  
$$L_i = R_{i-1}$$
$$R_i = L_{i-1} \oplus F(R_{i-1}, K_i)$$
- F takes 32-bit R half and 48-bit subkey:
  - expands R to 48-bits using perm E
  - adds to subkey using XOR
  - passes through 8 S-boxes to get 32-bit result
  - finally permutes using 32-bit perm P

# Encryption (IP, IP<sup>-1</sup>)

- IP

| Bit | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7 |
|-----|----|----|----|----|----|----|----|---|
| 1   | 58 | 50 | 42 | 34 | 26 | 18 | 10 | 2 |
| 9   | 60 | 52 | 44 | 36 | 28 | 20 | 12 | 4 |
| 17  | 62 | 54 | 46 | 38 | 30 | 22 | 14 | 6 |
| 25  | 64 | 56 | 48 | 40 | 32 | 24 | 16 | 8 |
| 33  | 57 | 49 | 41 | 33 | 25 | 17 | 9  | 1 |
| 41  | 59 | 51 | 43 | 35 | 27 | 19 | 11 | 3 |
| 49  | 61 | 53 | 45 | 37 | 29 | 21 | 13 | 5 |
| 57  | 63 | 55 | 47 | 39 | 31 | 23 | 15 | 7 |

- IP-1

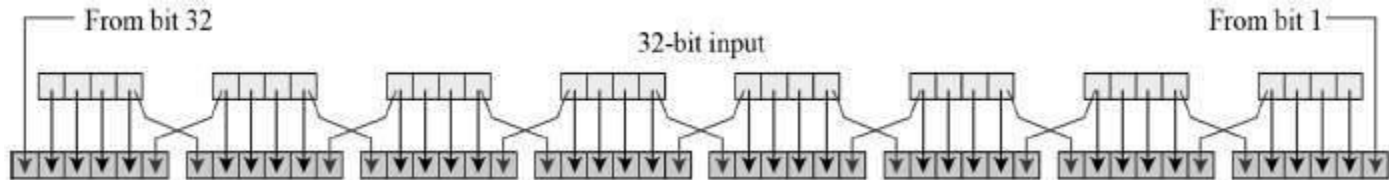
| Bit | 0  | 1 | 2  | 3  | 4  | 5  | 6  | 7  |
|-----|----|---|----|----|----|----|----|----|
| 1   | 40 | 8 | 48 | 16 | 56 | 24 | 64 | 32 |
| 9   | 39 | 7 | 47 | 15 | 55 | 23 | 63 | 31 |
| 17  | 38 | 6 | 46 | 14 | 54 | 22 | 62 | 30 |
| 25  | 37 | 5 | 45 | 13 | 53 | 21 | 61 | 29 |
| 33  | 36 | 4 | 44 | 12 | 52 | 20 | 60 | 28 |
| 41  | 35 | 3 | 43 | 11 | 51 | 19 | 59 | 27 |
| 49  | 34 | 2 | 42 | 10 | 50 | 18 | 58 | 26 |
| 57  | 33 | 1 | 41 | 9  | 49 | 17 | 57 | 25 |

■ Note: IP(IP-1) = IP-1(IP) = I

## Expansion /Permutation box

Since right input is 32-bit and round key is a 48-bit, we first need to expand right input to 48 bits.

Permutation logic is graphically depicted in the following illustration –



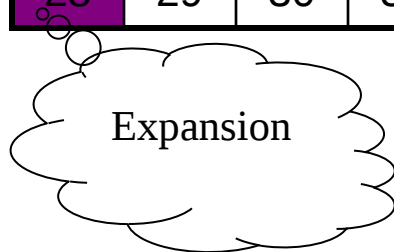
The graphically depicted permutation logic is generally described as table in DES specification illustrated as shown –

|    |    |    |    |    |    |
|----|----|----|----|----|----|
| 32 | 01 | 02 | 03 | 04 | 05 |
| 04 | 05 | 06 | 07 | 08 | 09 |
| 08 | 09 | 10 | 11 | 12 | 13 |
| 12 | 13 | 14 | 15 | 16 | 17 |
| 16 | 17 | 18 | 19 | 20 | 21 |
| 20 | 21 | 22 | 23 | 24 | 25 |
| 24 | 25 | 26 | 27 | 28 | 29 |
| 28 | 29 | 31 | 31 | 32 | 01 |

# Encryption (Round) (cont.)

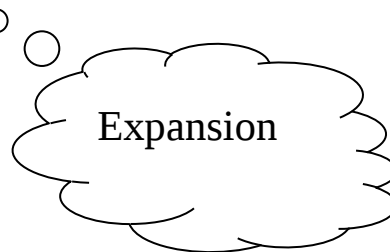
■ E

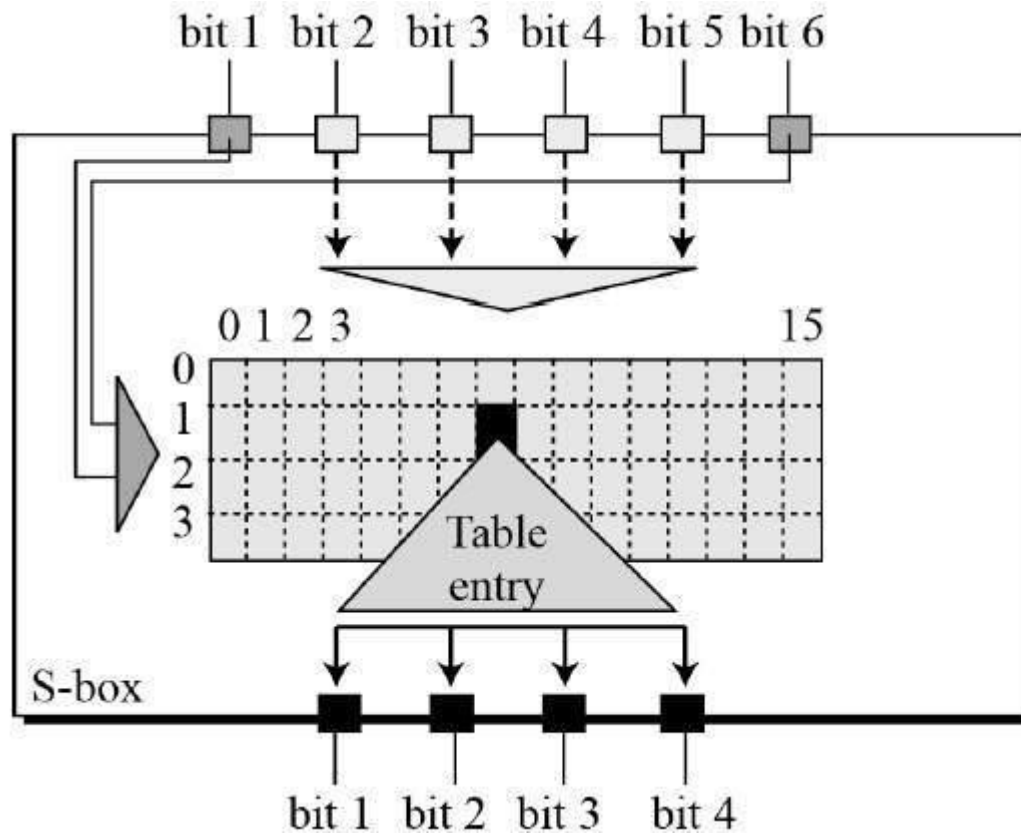
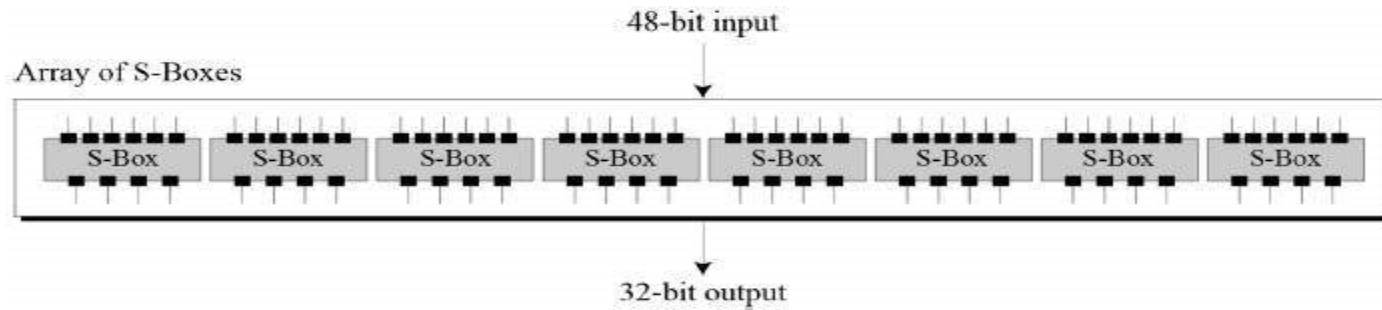
|    |    |    |    |    |    |
|----|----|----|----|----|----|
| 32 | 1  | 2  | 3  | 4  | 5  |
| 4  | 5  | 6  | 7  | 8  | 9  |
| 8  | 9  | 10 | 11 | 12 | 13 |
| 12 | 13 | 14 | 45 | 16 | 17 |
| 16 | 17 | 18 | 19 | 20 | 21 |
| 20 | 21 | 22 | 23 | 24 | 25 |
| 24 | 25 | 26 | 27 | 28 | 29 |
| 28 | 29 | 30 | 31 | 32 | 1  |



■ P

|    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|
| 16 | 7  | 20 | 21 | 29 | 12 | 28 | 17 |
| 1  | 15 | 23 | 26 | 5  | 18 | 31 | 10 |
| 2  | 8  | 24 | 14 | 32 | 27 | 3  | 9  |
| 9  | 13 | 30 | 6  | 22 | 11 | 4  | 25 |





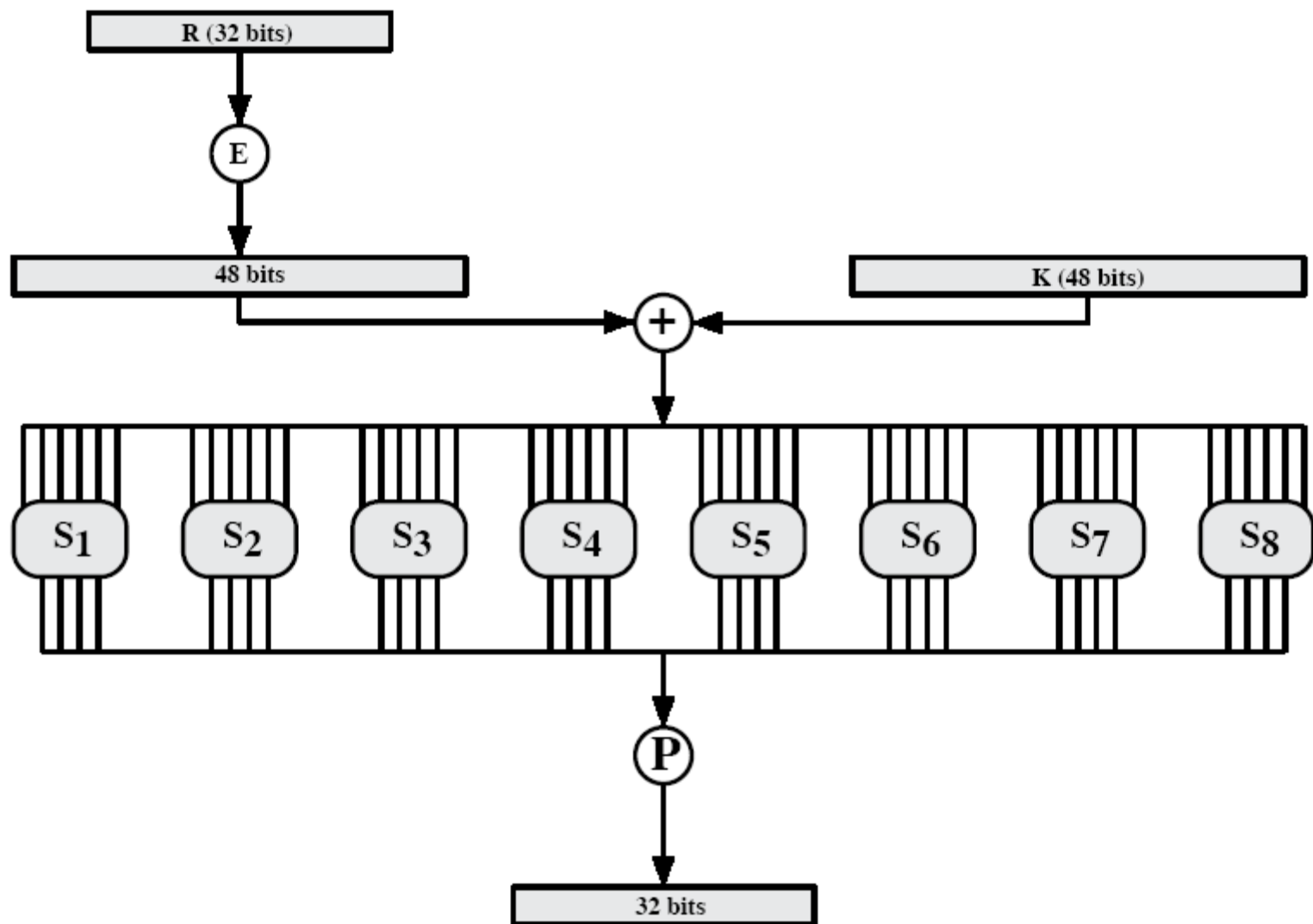


Figure 3.9 Calculation of  $F(R, K)$

# Encryption (Round) (cont.)

## S-box

$s_1$

|    |    |    |   |    |    |    |    |    |    |    |    |    |    |   |    |
|----|----|----|---|----|----|----|----|----|----|----|----|----|----|---|----|
| 14 | 4  | 13 | 1 | 2  | 15 | 11 | 8  | 3  | 10 | 6  | 12 | 5  | 9  | 0 | 7  |
| 0  | 15 | 7  | 4 | 14 | 2  | 13 | 1  | 10 | 6  | 12 | 11 | 9  | 5  | 3 | 8  |
| 4  | 1  | 14 | 8 | 13 | 6  | 2  | 11 | 15 | 12 | 9  | 7  | 3  | 10 | 5 | 0  |
| 15 | 12 | 8  | 2 | 4  | 9  | 1  | 7  | 5  | 11 | 3  | 14 | 10 | 0  | 6 | 13 |

$s_2$

|    |    |    |    |    |    |    |    |    |   |    |    |    |   |    |    |
|----|----|----|----|----|----|----|----|----|---|----|----|----|---|----|----|
| 15 | 1  | 8  | 14 | 6  | 11 | 3  | 4  | 9  | 7 | 2  | 13 | 12 | 0 | 5  | 10 |
| 3  | 13 | 4  | 7  | 15 | 2  | 8  | 14 | 12 | 0 | 1  | 10 | 6  | 9 | 11 | 5  |
| 0  | 14 | 7  | 11 | 10 | 4  | 13 | 1  | 5  | 8 | 12 | 6  | 9  | 3 | 2  | 15 |
| 13 | 8  | 10 | 1  | 3  | 15 | 4  | 2  | 11 | 6 | 7  | 12 | 0  | 5 | 14 | 9  |

$s_3$

|    |    |    |    |   |    |    |    |    |    |    |    |    |    |    |    |
|----|----|----|----|---|----|----|----|----|----|----|----|----|----|----|----|
| 10 | 0  | 9  | 14 | 6 | 3  | 15 | 5  | 1  | 13 | 12 | 7  | 11 | 4  | 2  | 8  |
| 13 | 7  | 0  | 9  | 3 | 4  | 6  | 10 | 2  | 8  | 5  | 14 | 12 | 11 | 15 | 1  |
| 13 | 6  | 4  | 9  | 8 | 15 | 3  | 0  | 11 | 1  | 2  | 12 | 5  | 10 | 14 | 7  |
| 1  | 10 | 13 | 0  | 6 | 9  | 8  | 7  | 4  | 15 | 14 | 3  | 11 | 5  | 2  | 12 |

$s_4$

|    |    |    |   |    |    |    |    |    |   |   |    |    |    |    |    |
|----|----|----|---|----|----|----|----|----|---|---|----|----|----|----|----|
| 7  | 13 | 14 | 3 | 0  | 6  | 9  | 10 | 1  | 2 | 8 | 5  | 11 | 12 | 4  | 15 |
| 13 | 8  | 11 | 5 | 6  | 15 | 0  | 3  | 4  | 7 | 2 | 12 | 1  | 10 | 14 | 9  |
| 10 | 6  | 9  | 0 | 12 | 11 | 7  | 13 | 15 | 1 | 3 | 14 | 5  | 2  | 8  | 4  |
| 3  | 15 | 0  | 6 | 10 | 1  | 13 | 8  | 9  | 4 | 5 | 11 | 12 | 7  | 2  | 14 |

$s_5$

|    |    |    |    |    |    |    |    |    |    |    |    |    |   |    |    |
|----|----|----|----|----|----|----|----|----|----|----|----|----|---|----|----|
| 2  | 12 | 4  | 1  | 7  | 10 | 11 | 6  | 8  | 5  | 3  | 15 | 13 | 0 | 14 | 9  |
| 14 | 11 | 2  | 12 | 4  | 7  | 13 | 1  | 5  | 0  | 15 | 10 | 3  | 9 | 8  | 6  |
| 4  | 2  | 1  | 11 | 10 | 13 | 7  | 8  | 15 | 9  | 12 | 5  | 6  | 3 | 0  | 14 |
| 11 | 8  | 12 | 7  | 1  | 14 | 2  | 13 | 6  | 15 | 0  | 9  | 10 | 4 | 5  | 3  |

$s_6$

|    |    |    |    |   |    |    |    |    |    |    |    |    |    |    |    |
|----|----|----|----|---|----|----|----|----|----|----|----|----|----|----|----|
| 12 | 1  | 10 | 15 | 9 | 2  | 6  | 8  | 0  | 13 | 3  | 4  | 14 | 7  | 5  | 11 |
| 10 | 15 | 4  | 2  | 7 | 12 | 9  | 5  | 6  | 1  | 13 | 14 | 0  | 11 | 3  | 8  |
| 9  | 14 | 15 | 5  | 2 | 8  | 12 | 3  | 7  | 0  | 4  | 10 | 1  | 13 | 11 | 6  |
| 4  | 3  | 2  | 12 | 9 | 5  | 15 | 10 | 11 | 14 | 1  | 7  | 6  | 0  | 8  | 13 |

$s_7$

|    |    |    |    |    |   |    |    |    |    |   |    |    |    |   |    |
|----|----|----|----|----|---|----|----|----|----|---|----|----|----|---|----|
| 4  | 11 | 2  | 14 | 15 | 0 | 8  | 13 | 3  | 12 | 9 | 7  | 5  | 10 | 6 | 1  |
| 13 | 0  | 11 | 7  | 4  | 9 | 1  | 10 | 14 | 3  | 5 | 12 | 2  | 15 | 8 | 6  |
| 1  | 4  | 11 | 13 | 12 | 3 | 7  | 14 | 10 | 15 | 6 | 8  | 0  | 5  | 9 | 2  |
| 6  | 11 | 13 | 8  | 1  | 4 | 10 | 7  | 9  | 5  | 0 | 15 | 14 | 2  | 3 | 12 |

$s_8$

|    |    |    |   |    |    |    |    |    |    |    |    |    |    |    |    |
|----|----|----|---|----|----|----|----|----|----|----|----|----|----|----|----|
| 13 | 2  | 8  | 4 | 6  | 15 | 11 | 1  | 10 | 9  | 3  | 14 | 5  | 0  | 12 | 7  |
| 1  | 15 | 13 | 8 | 10 | 3  | 7  | 4  | 12 | 5  | 6  | 11 | 0  | 14 | 9  | 2  |
| 7  | 11 | 4  | 1 | 9  | 12 | 14 | 2  | 0  | 6  | 10 | 13 | 15 | 3  | 5  | 8  |
| 2  | 1  | 14 | 7 | 4  | 10 | 8  | 13 | 15 | 12 | 9  | 0  | 3  | 5  | 6  | 11 |

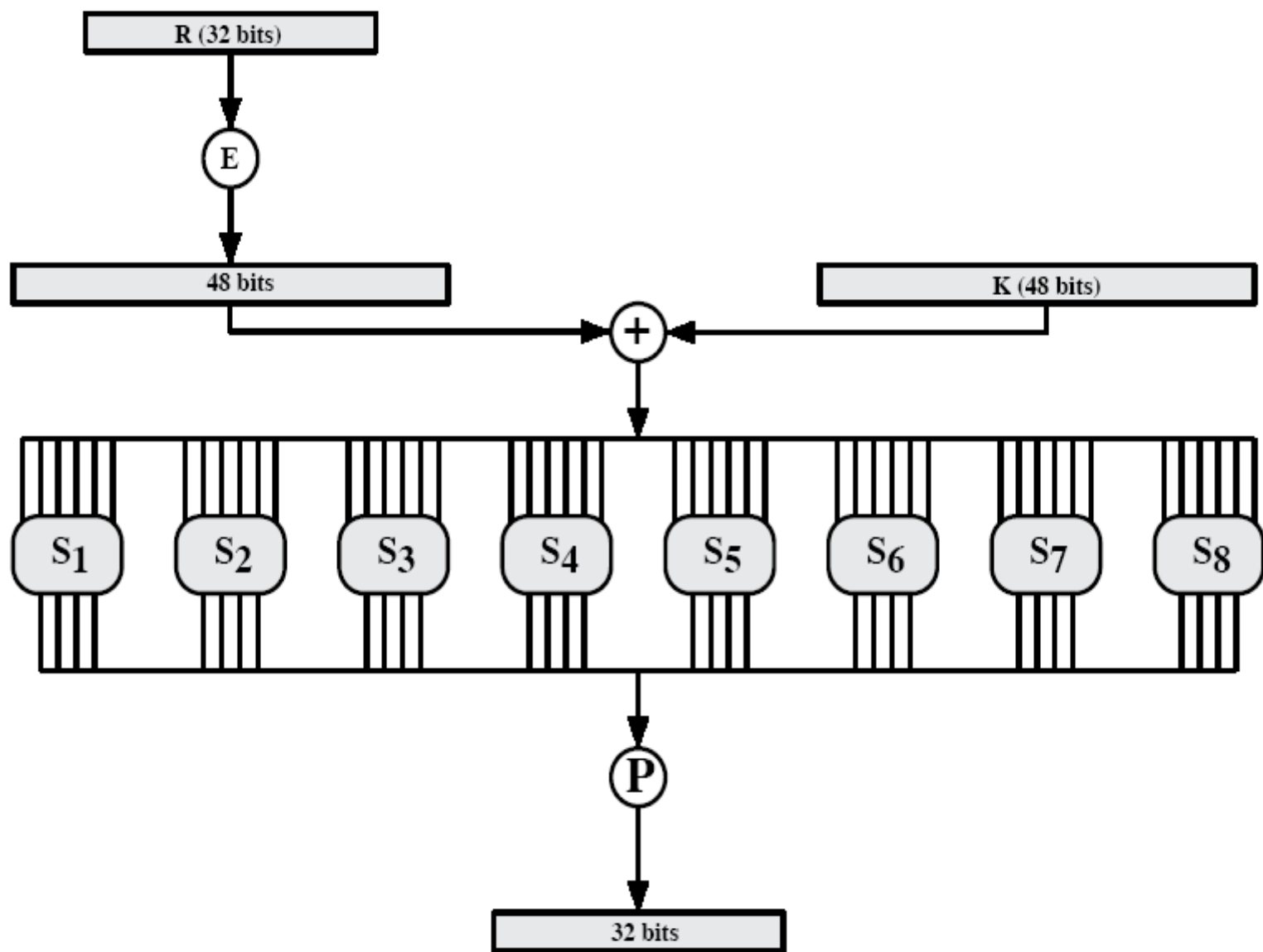


Figure 3.9 Calculation of  $F(R, K)$

# DES Key Schedule

- forms subkeys used in each round
  - initial permutation of the key (PC1) which selects 56-bits in two 28-bit halves
  - 16 stages consisting of:
    - rotating **each half** separately either 1 or 2 places depending on the **key rotation schedule K**
    - selecting 24-bits from each half & permuting them by PC2 for use in round function F
- **Concerns about:**
  - The algorithm and the key length (56-bits)

# DES Analysis

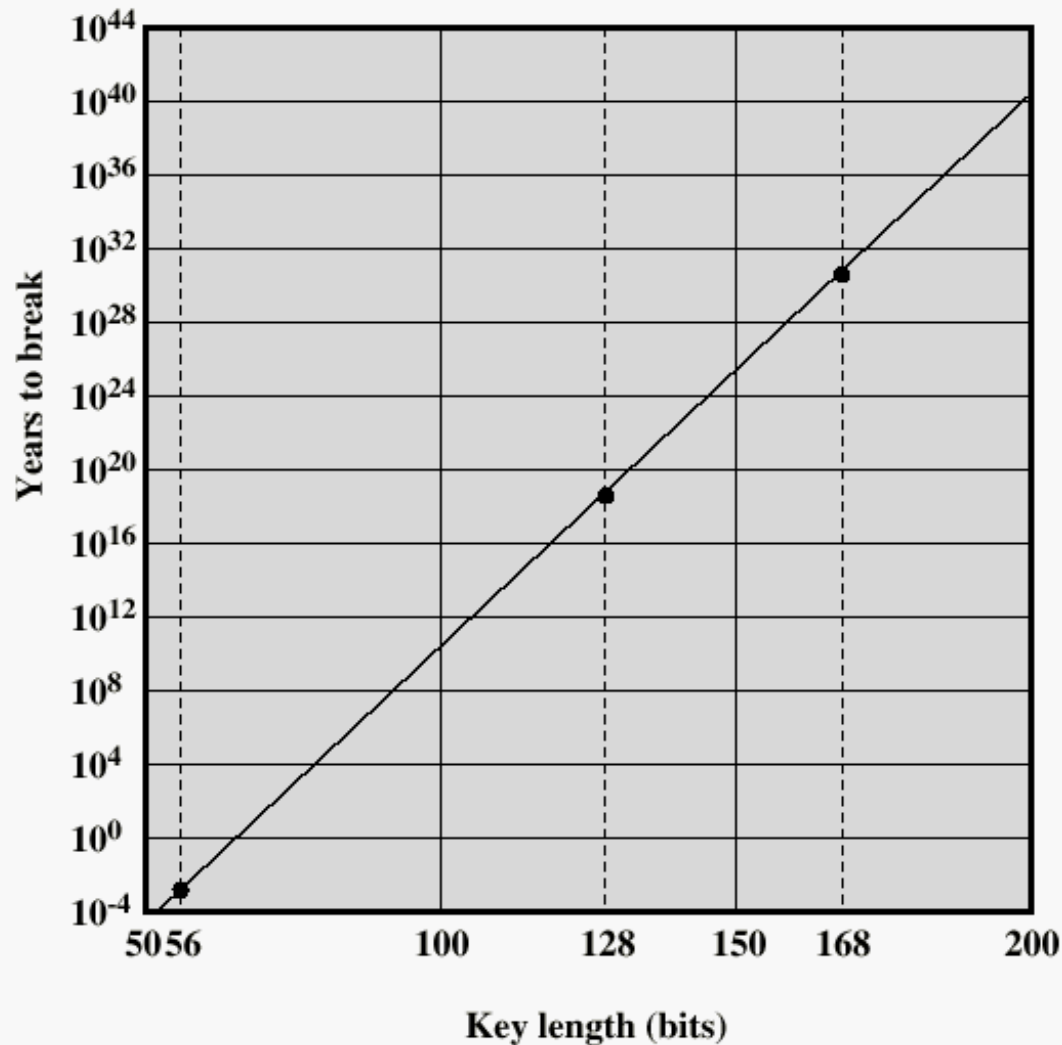
The DES satisfies both the desired properties of block cipher. These two properties make cipher very strong.

- **Avalanche effect** – A small change in plaintext results in the very great change in the ciphertext.
- **Completeness** – Each bit of ciphertext depends on many bits of plaintext.

During the last few years, cryptanalysis have found some weaknesses in DES when key selected are weak keys. These keys shall be avoided.

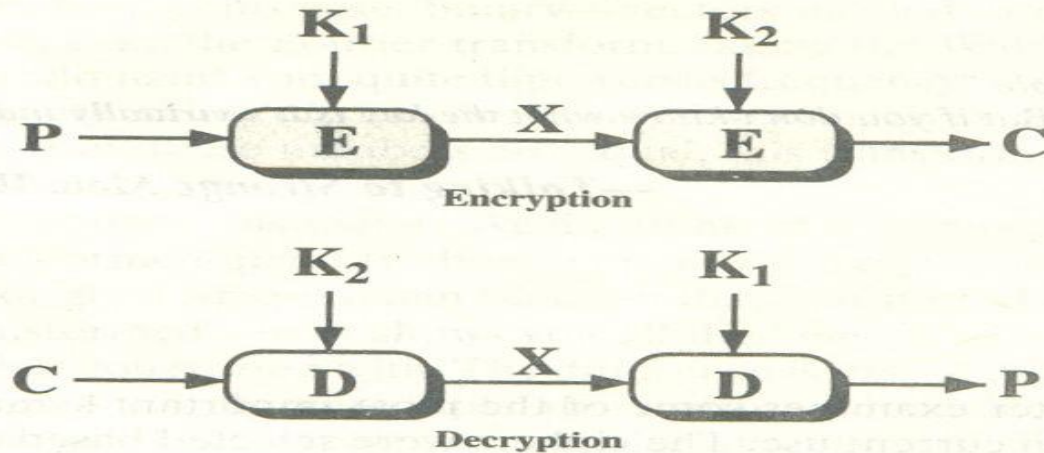
DES has proved to be a very well designed block cipher. There have been no significant cryptanalytic attacks on DES other than exhaustive key search.

# Time to break a code ( $10^6$ decryptions/ $\mu s$ )



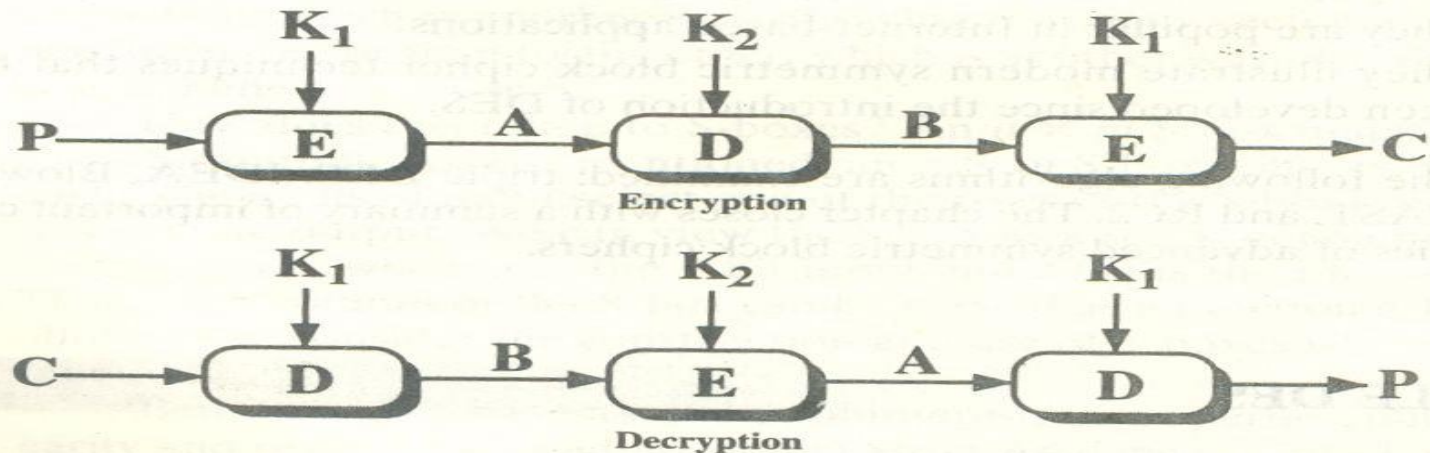
# Double DES and Triple DES

Double DES  
(or)  
Double DEA



(a) Double Encryption

Triple DES  
(or)  
Triple DEA  
With two  
keys



(b) Triple Encryption

# Triple DEA

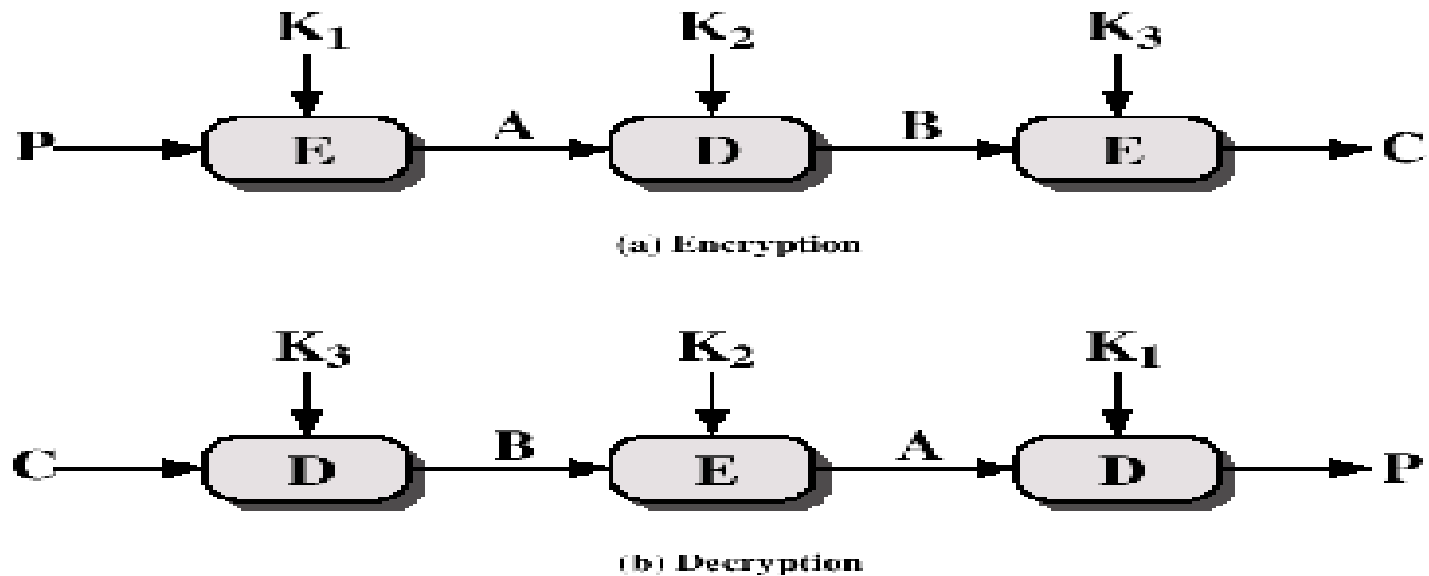
with 3 keys

- Use three keys and three executions of the DES algorithm (encrypt-decrypt-encrypt)

$$C = E_{K3}[D_{K2}[E_{K1}[P]]]$$

- $C$  = ciphertext
- $P$  = Plaintext
- $EK[X]$  = encryption of  $X$  using key  $K$
- $DK[Y]$  = decryption of  $Y$  using key  $K$
- Effective key length of 168 bits

# Triple DEA



**Figure 2.6 Triple DEA**

# **Advanced Encryption Standard (AES) Origins**

- **clear a replacement for DES was needed**
  - have theoretical attacks that can break it
  - have demonstrated exhaustive key search attacks
- **can use Triple-DES – but slow, has small blocks**
- **US NIST issued call for ciphers in 1997**
- **15 candidates accepted in Jun 98**
- **5 were shortlisted in Aug-99**
- **Rijndael was selected as the AES in Oct-2000**
- **issued as FIPS PUB 197 standard in Nov-2001**

# The AES Cipher - Rijndael

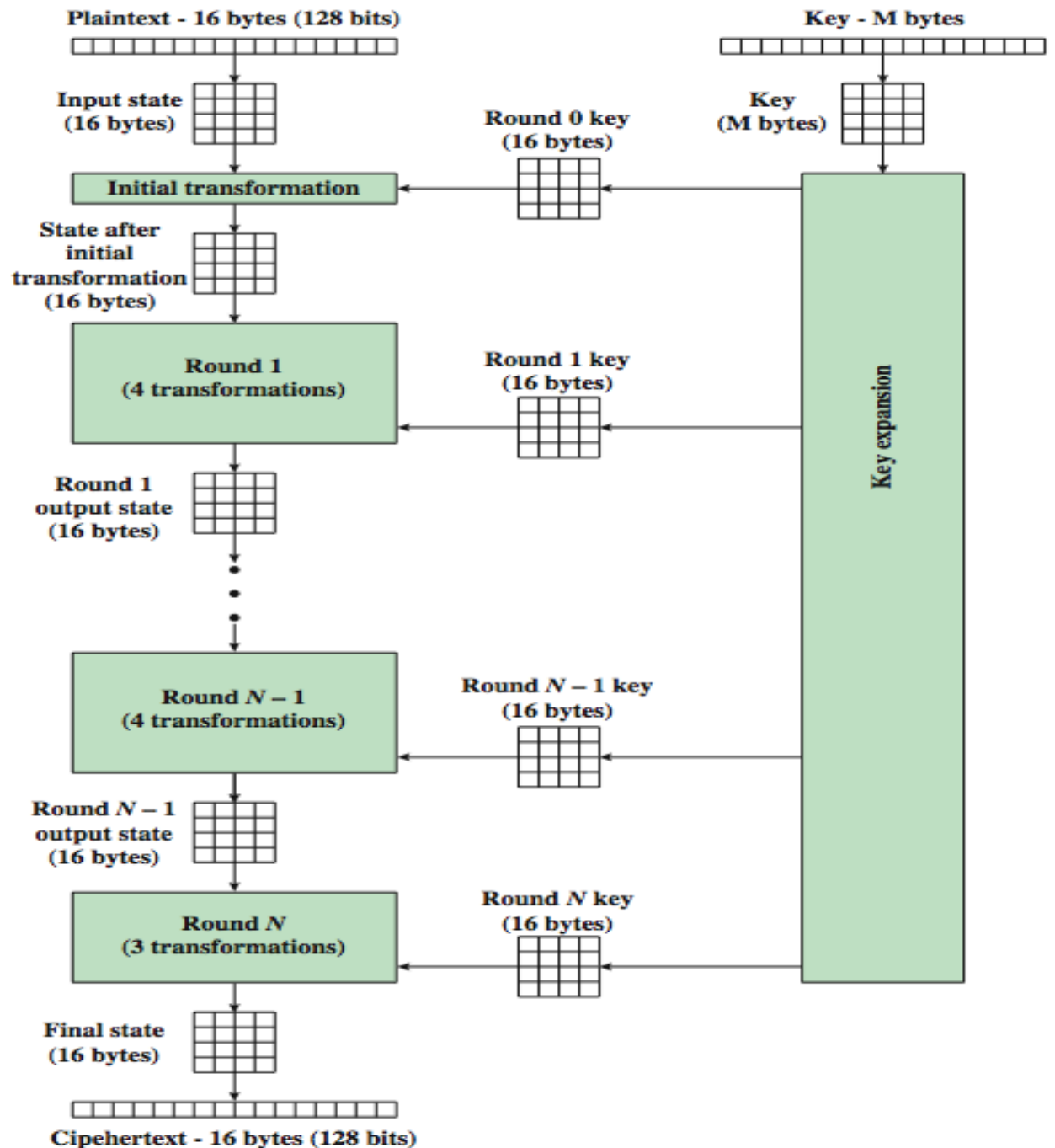
- designed by Rijmen-Daemen in Belgium
- Key: 128/192/256 bit keys,
- Plaintext: 128 bit data
- an **iterative** rather than **Feistel** cipher
  - processes data as block of 4 columns of 4 bytes
  - operates on **entire data block in every round**
- designed to have:
  - resistance against known attacks
  - speed and code compactness on many CPUs
  - design simplicity

# AES Structure

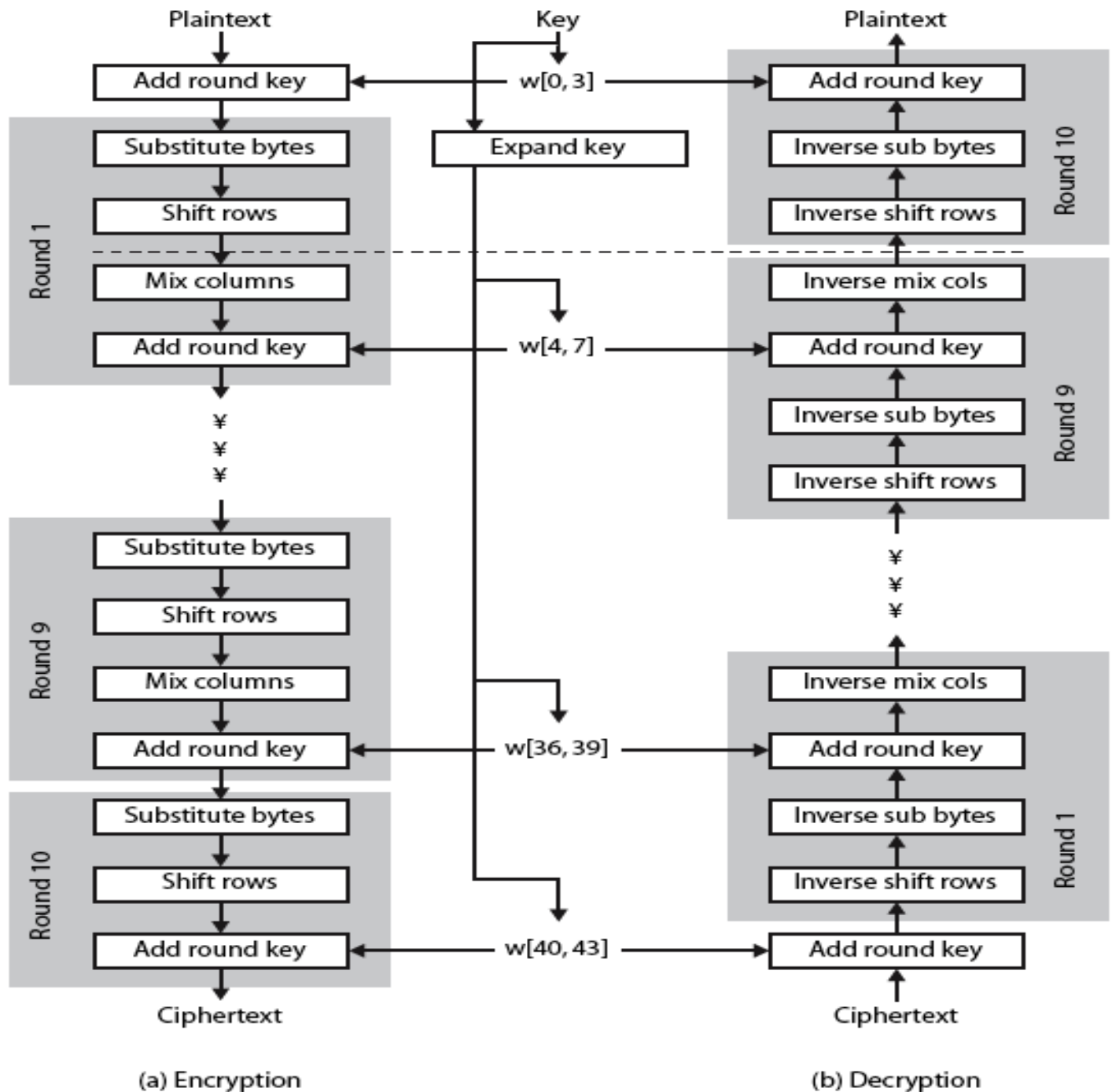
- data block of 4 columns of 4 bytes is state
- key is expanded to array of words
- has 9/11/13 rounds in which state undergoes:
  1. **byte substitution** (1 S-box used on every byte)
  2. **shift rows** (permute bytes between groups/columns)
  3. **mix columns** (subs using matrix multiply of groups)
  4. **add round key** (XOR state with key material)
  - **view as alternating XOR key & scramble data bytes**

| No.of rounds | Key Length (bytes) |
|--------------|--------------------|
| 10           | 16                 |
| 12           | 24                 |
| 14           | 32                 |

# AES Encryption Process



# AES Structure



# Some Comments on AES

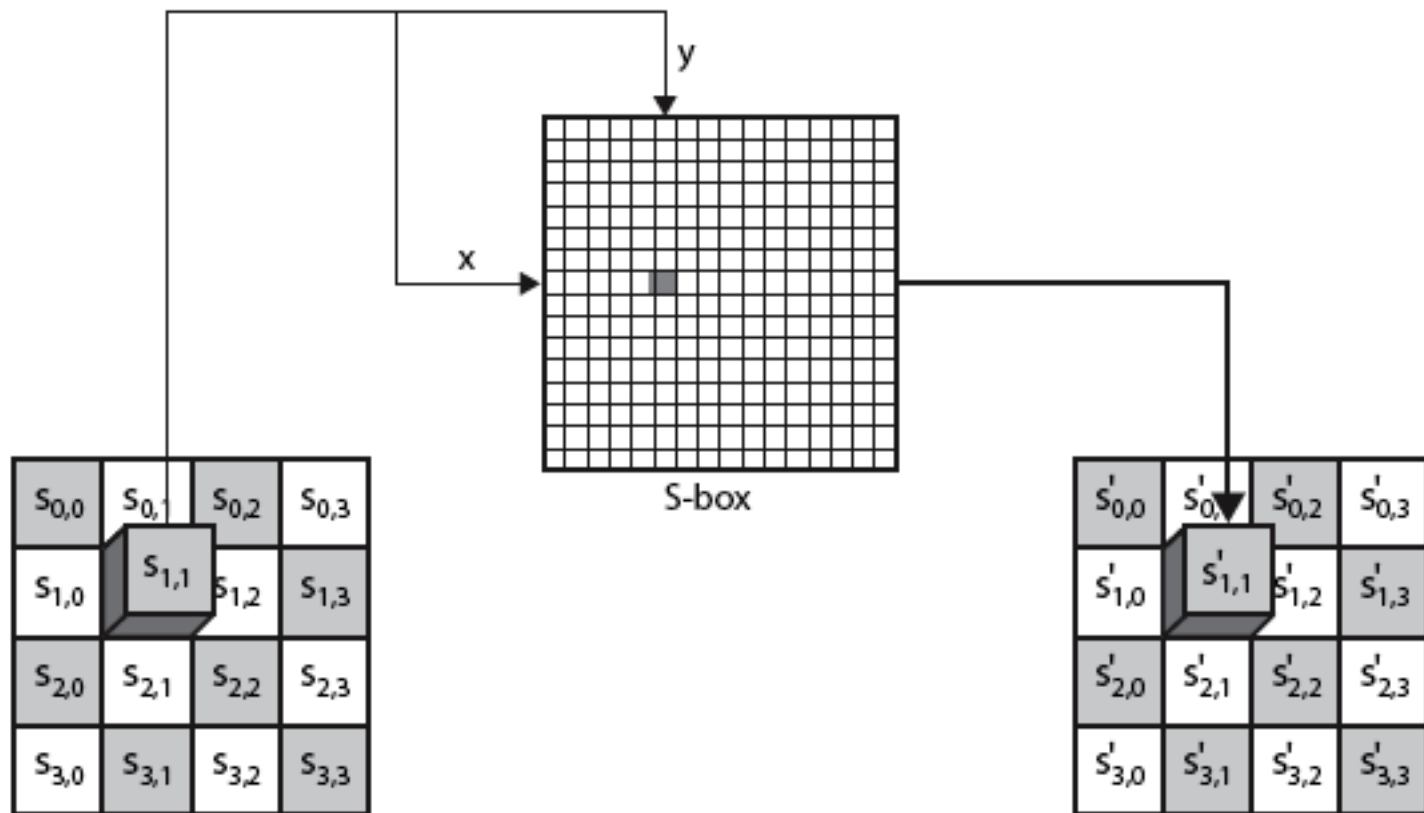
1. an iterative rather than Feistel cipher
2. key expanded into array of 32-bit words
  1. four words form round key in each round
3. 4 different stages are used as shown
4. has a simple structure
5. only AddRoundKey uses key
6. AddRoundKey a form of Vernam cipher
7. each stage is easily reversible
8. decryption uses keys in reverse order
9. decryption does recover plaintext
10. final round has only 3 stages

# Substitute Bytes

- a simple substitution of each byte
- uses one table of 16x16 bytes containing a permutation of all 256 8-bit values
- each byte of state is replaced by byte indexed by row (left 4-bits) & column (right 4-bits)
  - eg. byte {95} is replaced by byte in row 9 column 5
  - which has value {2A}
- S-box constructed using defined transformation of values
- designed to be resistant to all known attacks

|   | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | A  | B  | C  | D  | E  | F  |
|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 0 | 63 | 7C | 77 | 7B | F2 | 6B | 6F | C5 | 30 | 01 | 67 | 2B | FE | D7 | AB | 76 |
| 1 | CA | 82 | C9 | 7D | FA | 59 | 47 | F0 | AD | D4 | A2 | AF | 9C | A4 | 72 | C0 |
| 2 | B7 | FD | 93 | 26 | 36 | 3F | F7 | CC | 34 | A5 | E5 | F1 | 71 | D8 | 31 | 15 |
| 3 | 04 | C7 | 23 | C3 | 18 | 96 | 05 | 9A | 07 | 12 | 80 | E2 | EB | 27 | B2 | 75 |
| 4 | 09 | 83 | 2C | 1A | 1B | 6E | 5A | A0 | 52 | 3B | D6 | B3 | 29 | E3 | 2F | 84 |
| 5 | 53 | D1 | 00 | ED | 20 | FC | B1 | 5B | 6A | CB | BE | 39 | 4A | 4C | 58 | CF |
| 6 | D0 | EF | AA | FB | 43 | 4D | 33 | 85 | 45 | F9 | 02 | 7F | 50 | 3C | 9F | A8 |
| 7 | 51 | A3 | 40 | 8F | 92 | 9D | 38 | F5 | BC | B6 | DA | 21 | 10 | FF | F3 | D2 |
| 8 | CD | 0C | 13 | EC | 5F | 97 | 44 | 17 | C4 | A7 | 7E | 3D | 64 | 5D | 19 | 73 |
| 9 | 60 | 81 | 4F | DC | 22 | 2A | 90 | 88 | 46 | EE | B8 | 14 | DE | 5E | 0B | DB |
| A | E0 | 32 | 3A | 0A | 49 | 06 | 24 | 5C | C2 | D3 | AC | 62 | 91 | 95 | E4 | 79 |
| B | E7 | C8 | 37 | 6D | 8D | D5 | 4E | A9 | 6C | 56 | F4 | EA | 65 | 7A | AE | 08 |
| C | BA | 78 | 25 | 2E | 1C | A6 | B4 | C6 | E8 | DD | 74 | 1F | 4B | BD | 8B | 8A |
| D | 70 | 3E | B5 | 66 | 48 | 03 | F6 | 0E | 61 | 35 | 57 | B9 | 86 | C1 | 1D | 9E |
| E | E1 | F8 | 98 | 11 | 69 | D9 | 8E | 94 | 9B | 1E | 87 | E9 | CE | 55 | 28 | DF |
| F | 8C | A1 | 89 | 0D | BF | E6 | 42 | 68 | 41 | 99 | 2D | 0F | B0 | 54 | BB | 16 |

# Substitute Bytes



**Substitute Bytes Example** →

|    |    |    |    |
|----|----|----|----|
| EA | 04 | 65 | 85 |
| 83 | 45 | 5D | 96 |
| 5C | 33 | 98 | B0 |
| F0 | 2D | AD | C5 |

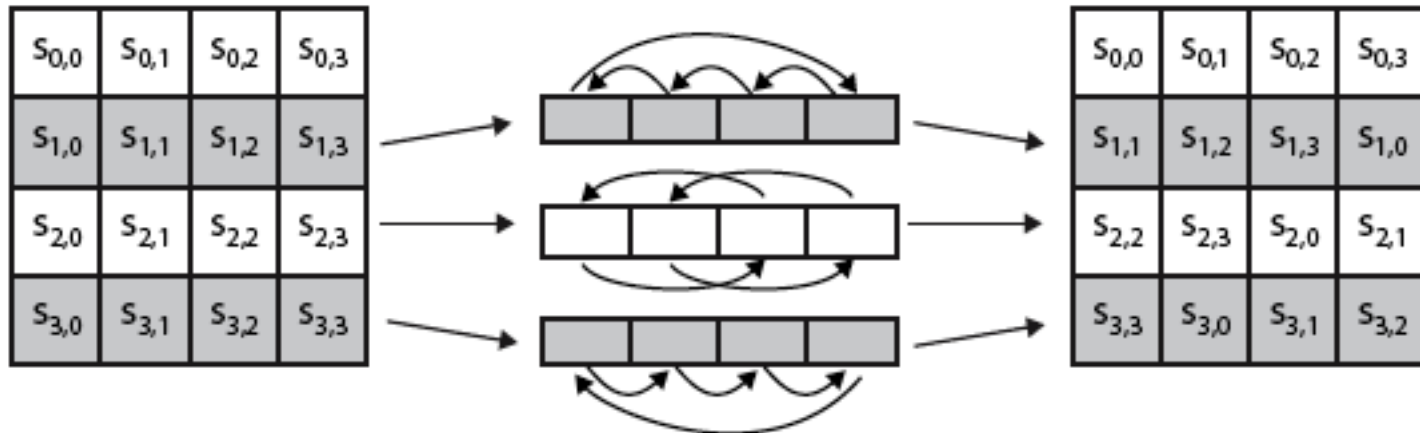


|    |    |    |    |
|----|----|----|----|
| 87 | F2 | 4D | 97 |
| EC | 6E | 4C | 90 |
| 4A | C3 | 46 | E7 |
| 8C | D8 | 95 | A6 |

# Shift Rows

- a circular byte shift in each row
  - 1st row is unchanged
  - 2nd row does 1 byte circular shift to left
  - 3rd row does 2 byte circular shift to left
  - 4th row does 3 byte circular shift to left
- decrypt inverts using shifts to right
- since state is processed by columns, this step permutes bytes between the columns

# Shift Rows



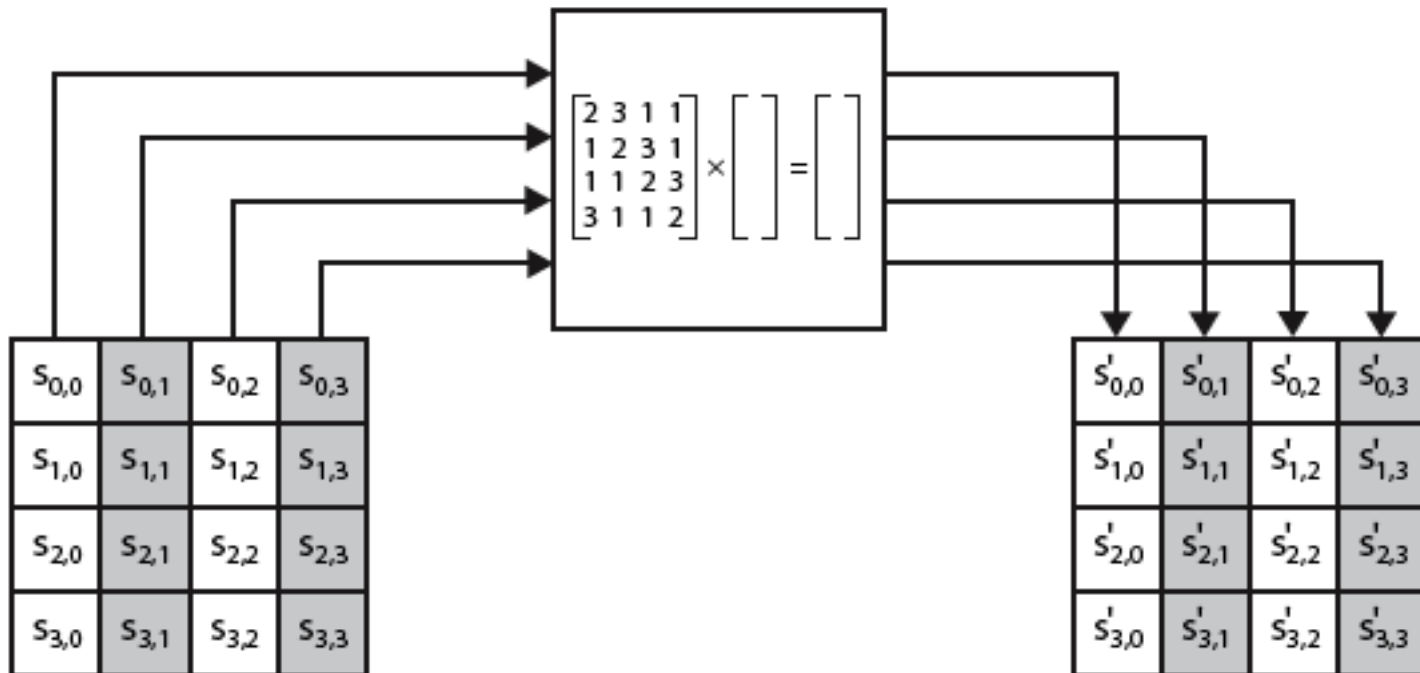
|    |    |    |    |
|----|----|----|----|
| 87 | F2 | 4D | 97 |
| EC | 6E | 4C | 90 |
| 4A | C3 | 46 | E7 |
| 8C | D8 | 95 | A6 |

→

|    |    |    |    |
|----|----|----|----|
| 87 | F2 | 4D | 97 |
| 6E | 4C | 90 | EC |
| 46 | E7 | 4A | C3 |
| A6 | 8C | D8 | 95 |

# Mix Columns

- each column is processed separately
- each byte is replaced by a value dependent on all 4 bytes in the column



$$\begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix} \begin{bmatrix} s_{0,0} & s_{0,1} & s_{0,2} & s_{0,3} \\ s_{1,0} & s_{1,1} & s_{1,2} & s_{1,3} \\ s_{2,0} & s_{2,1} & s_{2,2} & s_{2,3} \\ s_{3,0} & s_{3,1} & s_{3,2} & s_{3,3} \end{bmatrix} = \begin{bmatrix} s'_{0,0} & s'_{0,1} & s'_{0,2} & s'_{0,3} \\ s'_{1,0} & s'_{1,1} & s'_{1,2} & s'_{1,3} \\ s'_{2,0} & s'_{2,1} & s'_{2,2} & s'_{2,3} \\ s'_{3,0} & s'_{3,1} & s'_{3,2} & s'_{3,3} \end{bmatrix}$$

# Mix Columns Example

|    |    |    |    |
|----|----|----|----|
| 87 | F2 | 4D | 97 |
| 6E | 4C | 90 | EC |
| 46 | E7 | 4A | C3 |
| A6 | 8C | D8 | 95 |

→

|    |    |    |    |
|----|----|----|----|
| 47 | 40 | A3 | 4C |
| 37 | D4 | 70 | 9F |
| 94 | E4 | 3A | 42 |
| ED | A5 | A6 | BC |

$$(\{02\} \cdot \{87\}) \oplus (\{03\} \cdot \{6E\}) \oplus \{46\} \oplus \{A6\} = \{47\}$$

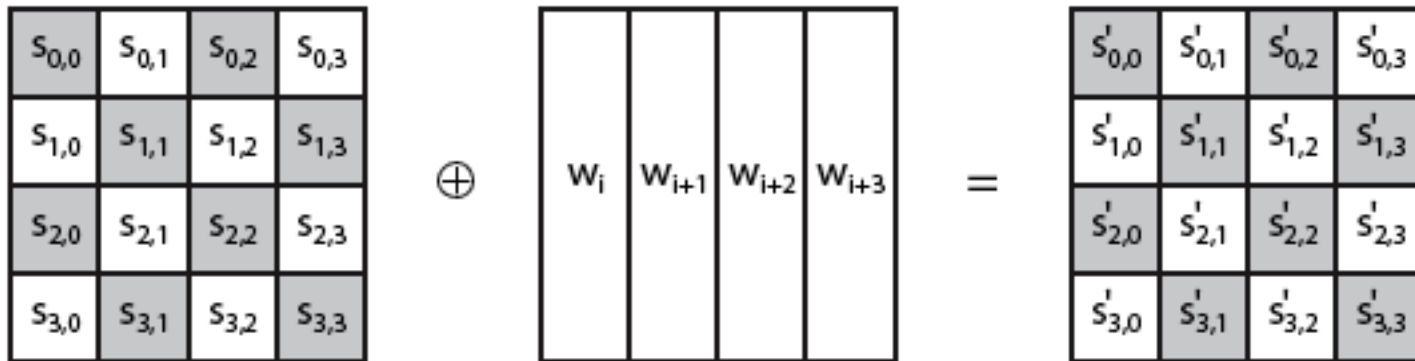
$$\{87\} \oplus (\{02\} \cdot \{6E\}) \oplus (\{03\} \cdot \{46\}) \oplus \{A6\} = \{37\}$$

$$\{87\} \oplus \{6E\} \oplus (\{02\} \cdot \{46\}) \oplus (\{03\} \cdot \{A6\}) = \{94\}$$

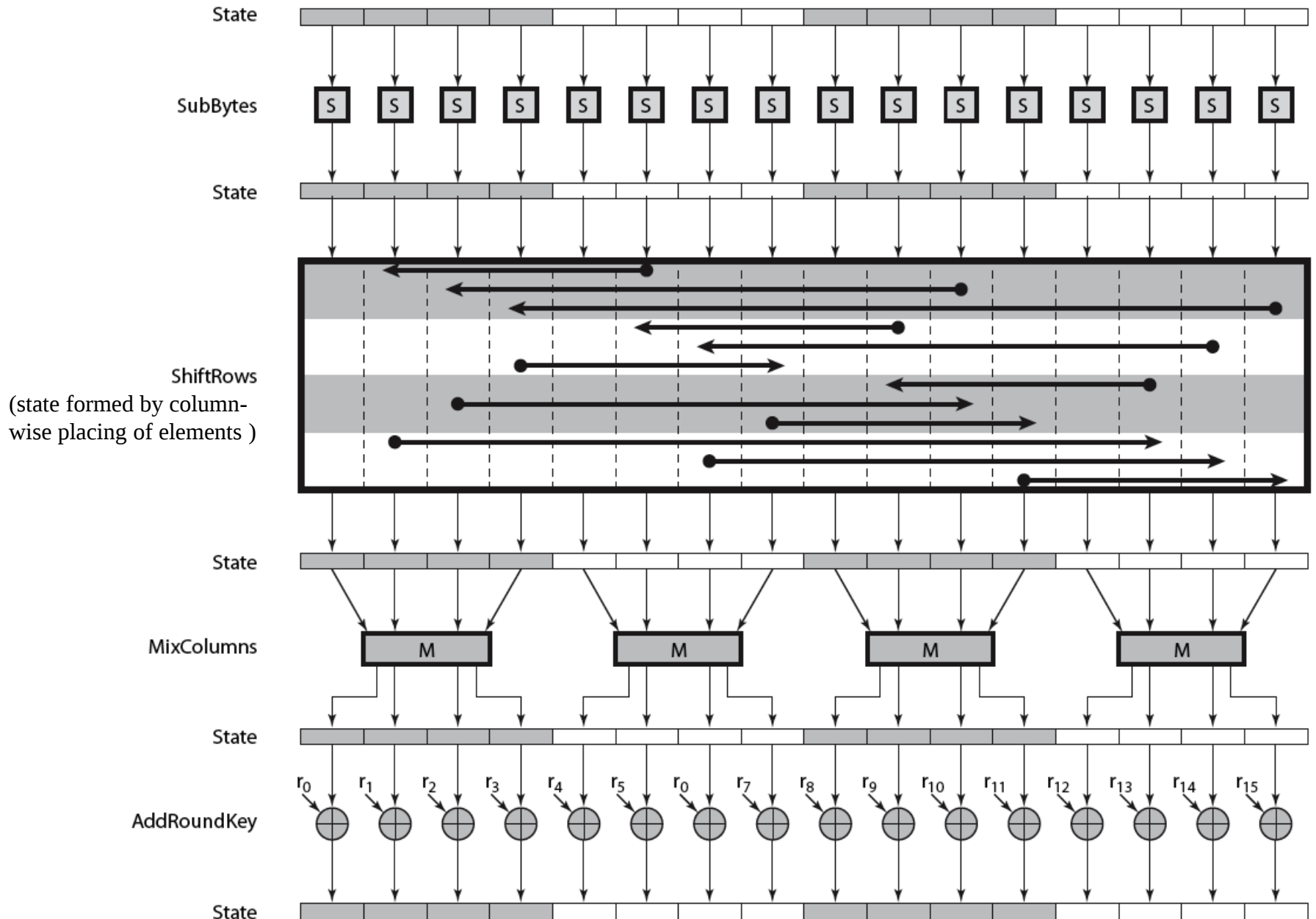
$$(\{03\} \cdot \{87\}) \oplus \{6E\} \oplus \{46\} \oplus (\{02\} \cdot \{A6\}) = \{ED\}$$

# Add Round Key

- XOR state with 128-bits of the round key
- again processed by column (though effectively a series of byte operations)
- inverse for decryption identical
  - since XOR own inverse, with reversed keys
- designed to be as simple as possible
  - a form of Vernam cipher on expanded key
  - requires other stages for complexity / security



# AES Round



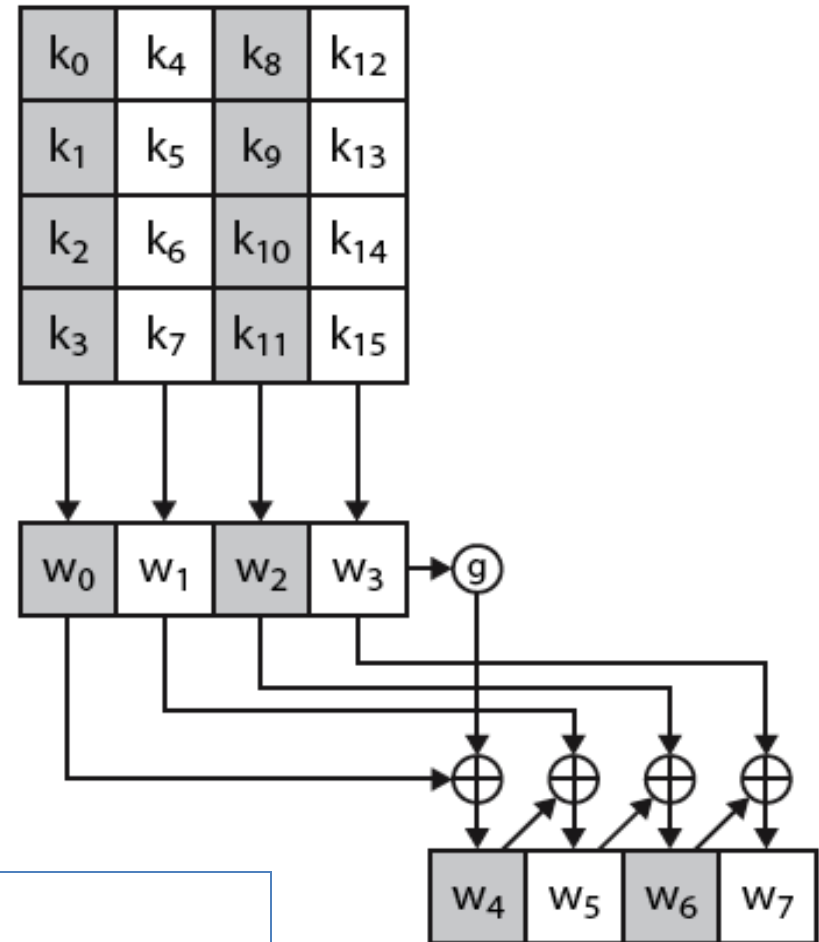
# AES Key Expansion

➤ takes 128-bit (16-byte) key and expands into array of 44/52/60 32-bit words

1. start by copying key into first 4 words
2. then loop creating words that depend on values in previous & 4 places back
  - ✓ in 3 of 4 cases just XOR these together
  - ✓ 1st word in 4 has rotate + S-box + XOR round constant on previous, before XOR 4th back

$$w_i = w_{i-1} \text{ xor } w_{i-4} \mid \text{if } i \neq \text{multiple of } 4$$

$$g = \text{S-Box}(\text{LCS}(w_3)) \text{ xor RoundConstant}_i$$



# Key Expansion Rationale

- designed to resist known attacks
- design criteria included
  - knowing part key insufficient to find many more
  - invertible transformation
  - fast on wide range of CPU's
  - use round constants to break symmetry
  - diffuse key bits into round keys
  - enough non-linearity to hinder analysis
  - simplicity of description

# Other Symmetric Block Ciphers

- **International Data Encryption Algorithm (IDEA)**
  - 128-bit key
  - Used in PGP
- **Blowfish** (A variant of DES with S-Box having values that are both random and key dependant)
  - Easy to implement
  - High execution speed
  - Run in less than 5K of memory

# Other Symmetric Block Ciphers

- **RC5**
  - Variable number of rounds
  - Data-dependent rotations
  - Variable-length key
  - Suitable for hardware and software
  - Fast, simple
  - Adaptable to processors of different word lengths
  - Low memory requirement
  - High security
- **Cast-128**
  - Key size from 40 to 128 bits
  - The round function differs from round to round

**Table 2.3 Conventional Encryption Algorithms**

| Algorithm  | Key Size (bits)  | Block Size (bits) | Number of Rounds | Applications                          |
|------------|------------------|-------------------|------------------|---------------------------------------|
| DES        | 56               | 64                | 16               | SET, Kerberos                         |
| Triple DES | 112 or 168       | 64                | 48               | Financial key management, PGP, S/MIME |
| AES        | 128, 192, or 256 | 128               | 10, 12, or 14    | Intended to replace DES and 3DES      |
| IDEA       | 128              | 64                | 8                | PGP                                   |
| Blowfish   | variable to 448  | 64                | 16               | Various software packages             |
| RC5        | variable to 2048 | 64                | variable to 255  | Various software packages             |

# **Cipher Block Modes of Operation**

# Encrypting a Large Message

1. **Electronic Code Book (ECB)**
2. **Cipher Block Chaining (CBC)**
3. **Output Feedback Mode (OFB)**
4. **Cipher Feedback Mode (CFB)**
5. **Counter Mode**

# Electronic Code Book (ECB)

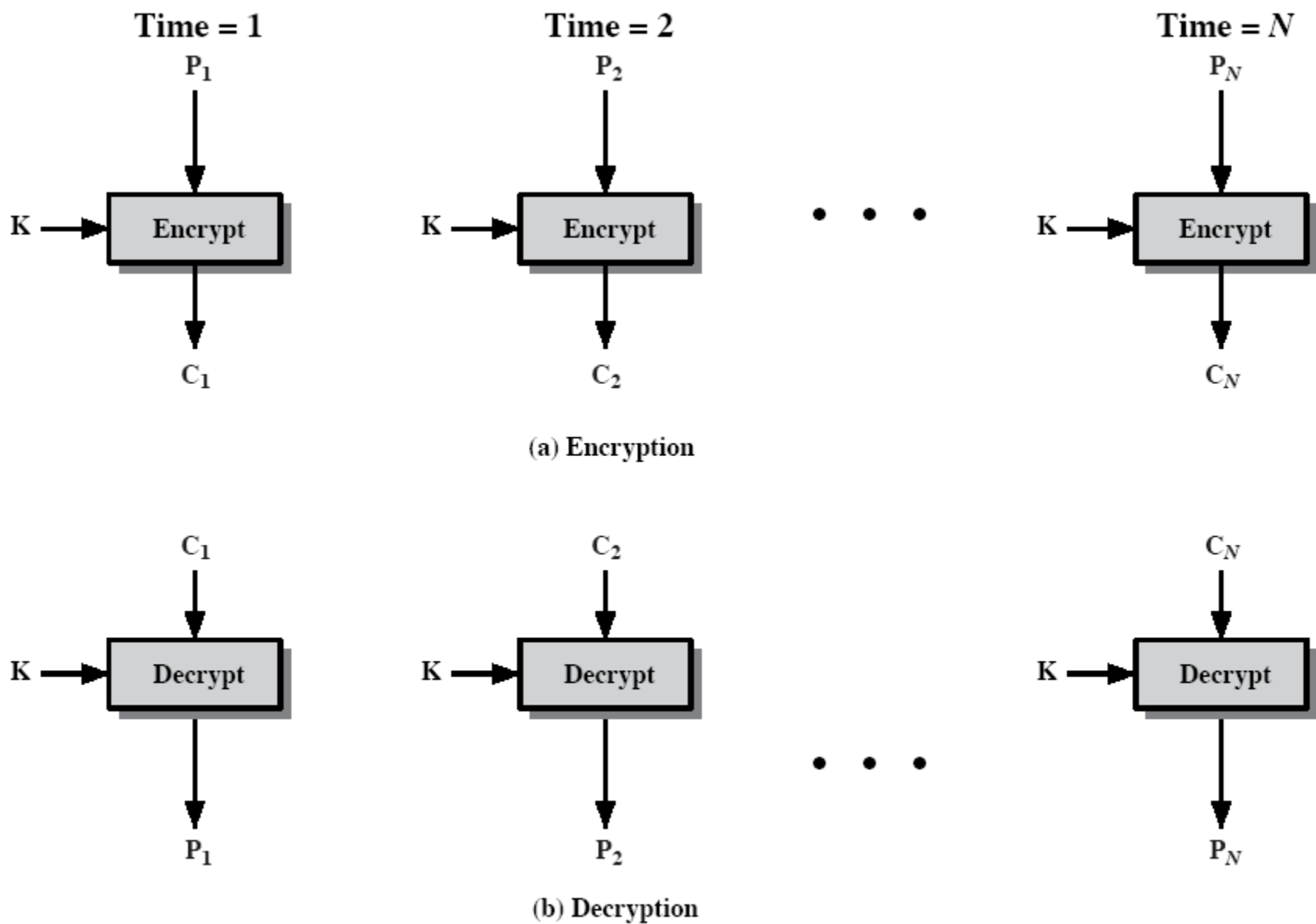
Break the message into 64-bit blocks (padding the last one) and encrypt each block with the secret key.

## *Two problems:*

1. two identical plain text block produce two identical cipher blocks
2. blocks can be rearranged or modified.

## **Example:** An eavesdropper:

1. can see which sets of employees have identical or similar salaries and
2. he can alter his own salary to match another employee with higher salary.



**Figure 3.11 Electronic Codebook (ECB) Mode**

# ECB Scheme

Encryption:  $C_i = E_K (P_i)$

Decryption:  $P_i = D_K (C_i)$

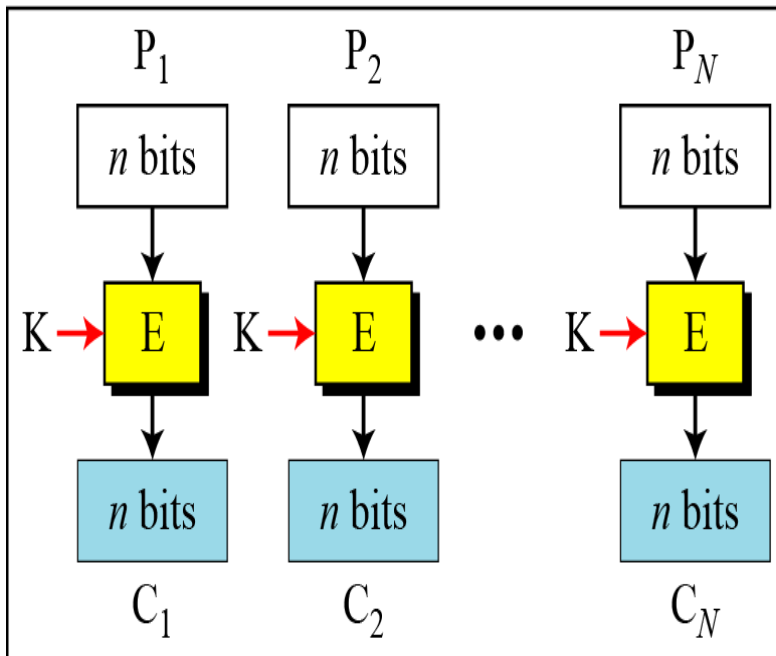
E: Encryption

D: Decryption

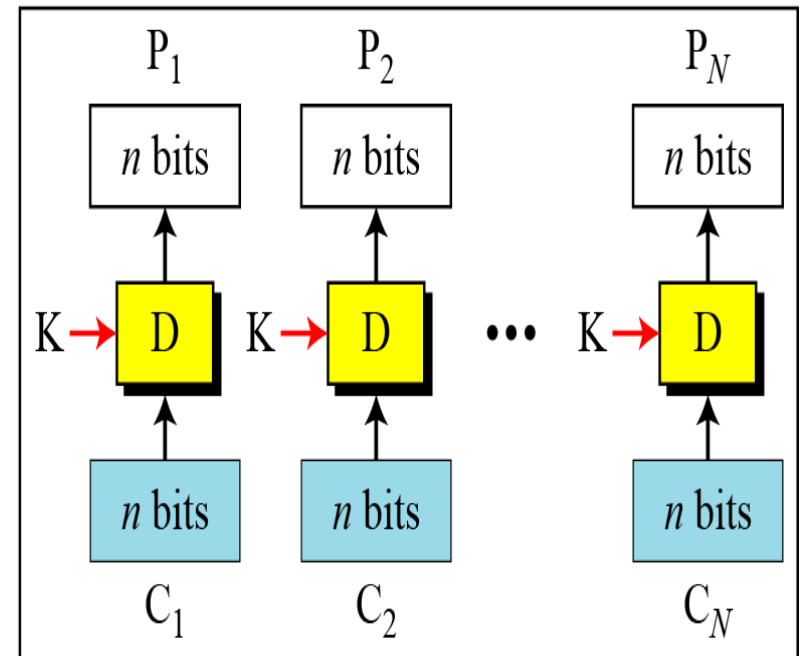
$P_i$ : Plaintext block  $i$

$C_i$ : Ciphertext block  $i$

K: Secret key



Encryption



Decryption

# Remarks on ECB

## *Advantages*

1. As we can process each block of plaintext independently of each other, we can process multiple blocks simultaneously.
2. If any plaintext or ciphertext blocks lost, it does not affect on the output of other blocks.
3. Parallel processing during encryption as well as decryption helps to increase the speed and the performance of the algorithm.

## *Disadvantages*

If two plaintext blocks are identical, then the ciphertext block generated are also same. Therefore, known plaintext attack is possible.

- Typical application:
  - secure transmission of short pieces of information (e.g. a temporary encryption key)

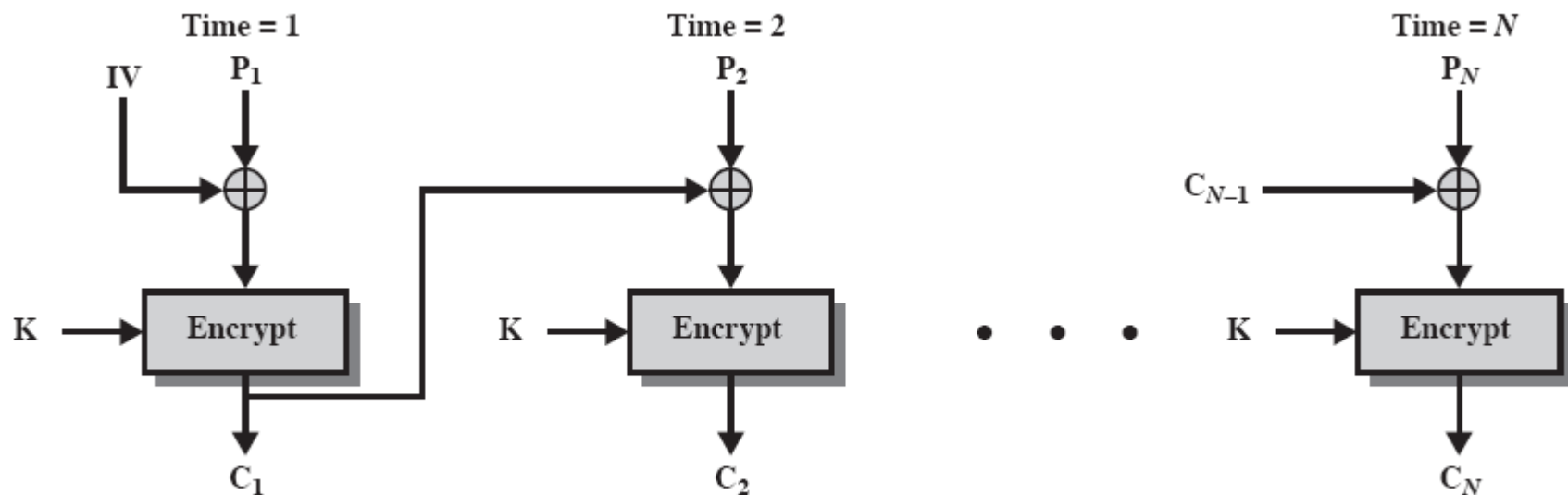
# Cipher Block Chaining (CBC)

- Solve security deficiencies in ECB
  - Repeated same plaintext block result different ciphertext block
- Each previous cipher blocks is chained to be input with current plaintext block, hence name
- Use Initialization (or Initial) Vector (IV) to start process

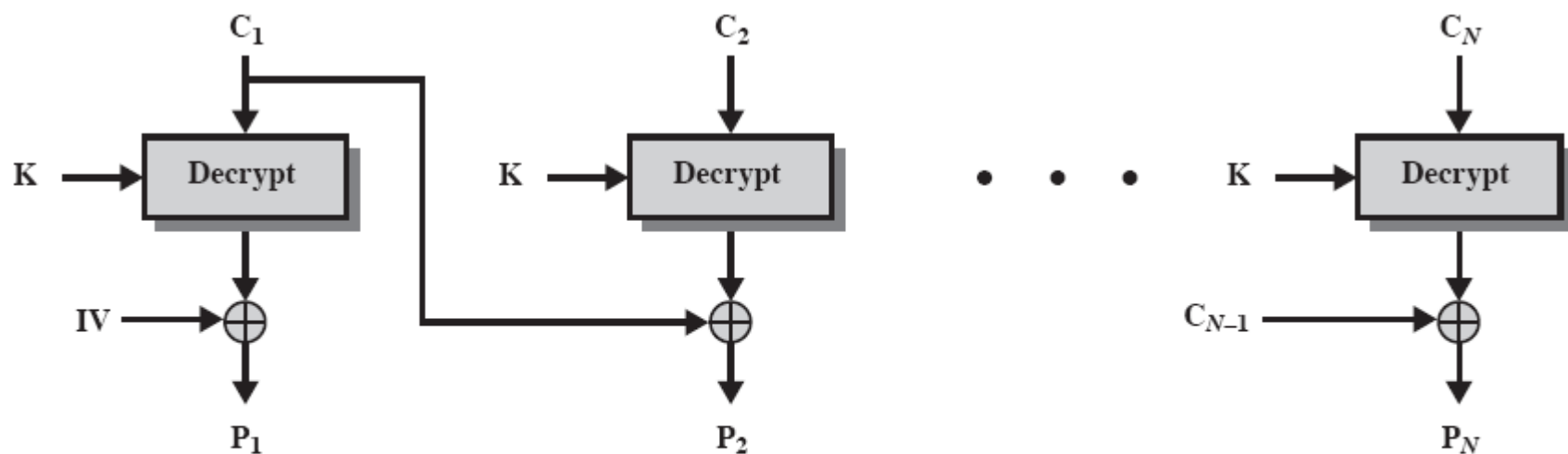
$$C_i = E_K (P_i \text{ XOR } C_{i-1})$$

$$C_0 = IV$$

- Uses: bulk data encryption, authentication



(a) Encryption



(b) Decryption

Figure 3.12 Cipher Block Chaining (CBC) Mode

# Remarks on CBC

## *Advantages*

1. For identical blocks of plaintext, different ciphertext blocks are generated. So, CBC is more secure as compared to ECB mode.
2. Hash value, i.e., last ciphertext block, helps to identify if the message is original or modified.

## *Disadvantages*

1. Parallel operation cannot be performed. So, it is slower as compared to ECB.
  2. Lost/missing of any block of ciphertext stops the decryption process of the remaining blocks.
- Initialization Vector (IV)
    - May sent encrypted in ECB mode before the rest of ciphertext

# Cipher FeedBack (CFB)

- Use Initial Vector to start process
- Encrypt previous ciphertext , then combined with the plaintext block using X-OR to produce the current ciphertext
- Cipher is fed back (hence name) to concatenate with the rest of IV
- Plaintext is treated as a stream of bits
  - Any number of bit (1, 8 or 64 or whatever) to be feed back (denoted CFB-1, CFB-8, CFB-64)
- Relation between plaintext and ciphertext
$$C_i = P_i \text{ XOR } \text{SelectLeft}(E_K(\text{ShiftLeft}(C_{i-1})))$$
$$C_0 = \text{IV}$$
- Uses: stream data encryption, authentication

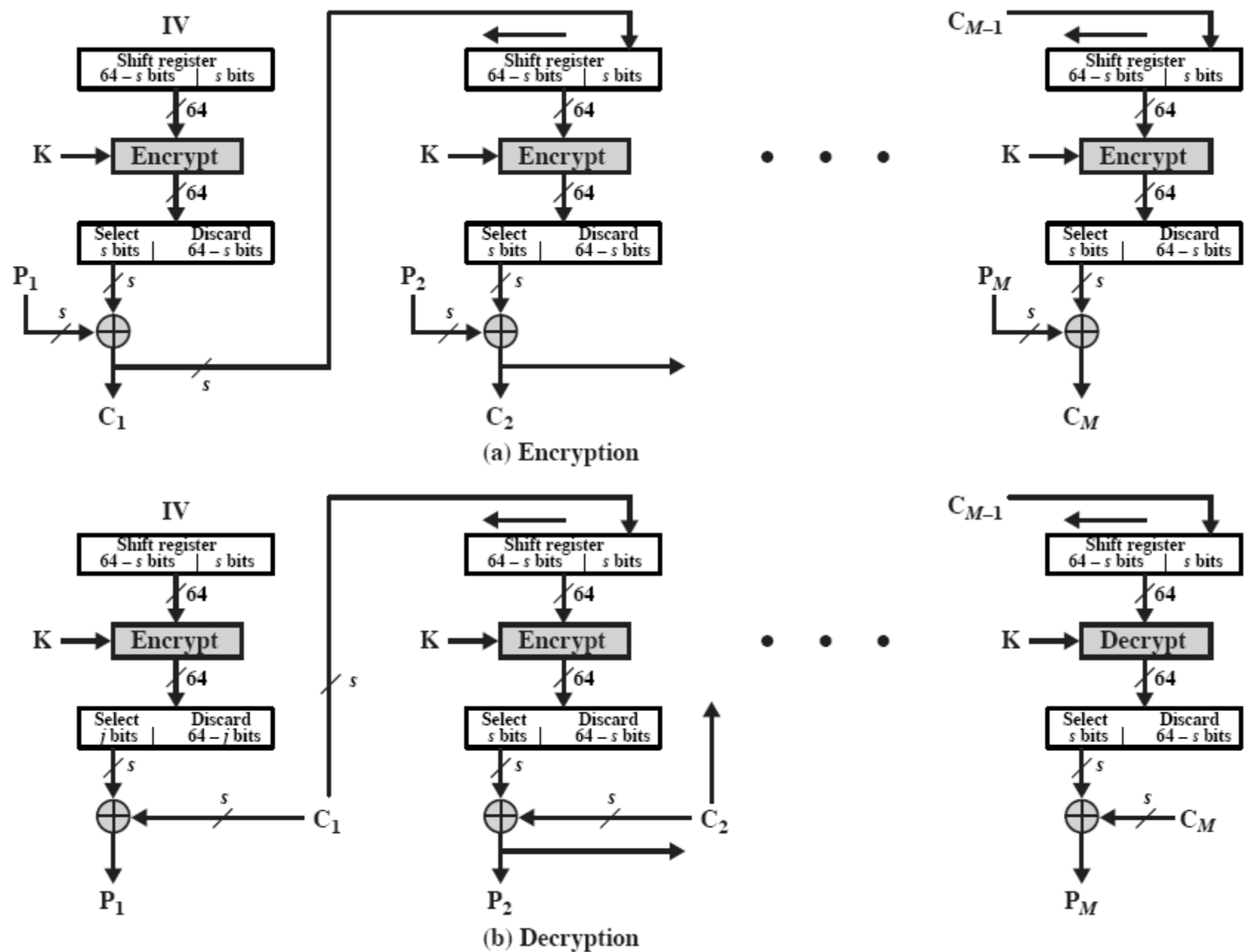


Figure 3.13  $s$ -bit Cipher Feedback (CFB) Mode

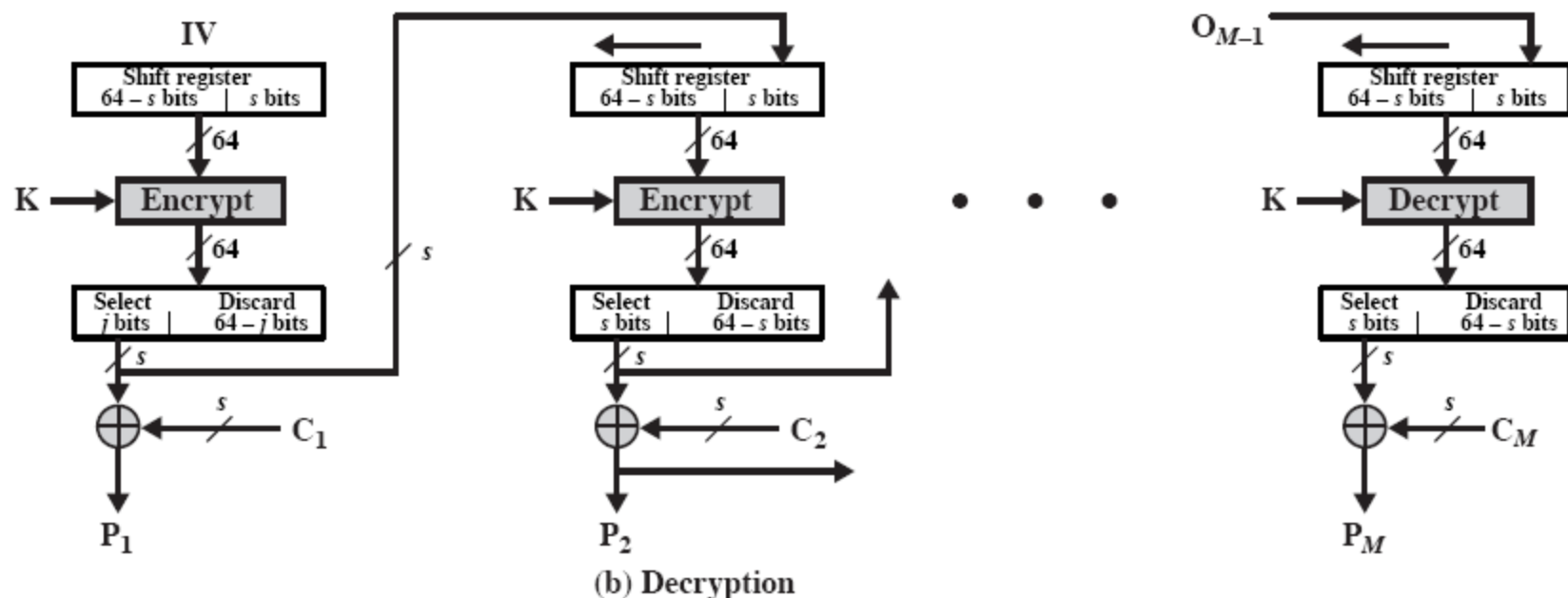
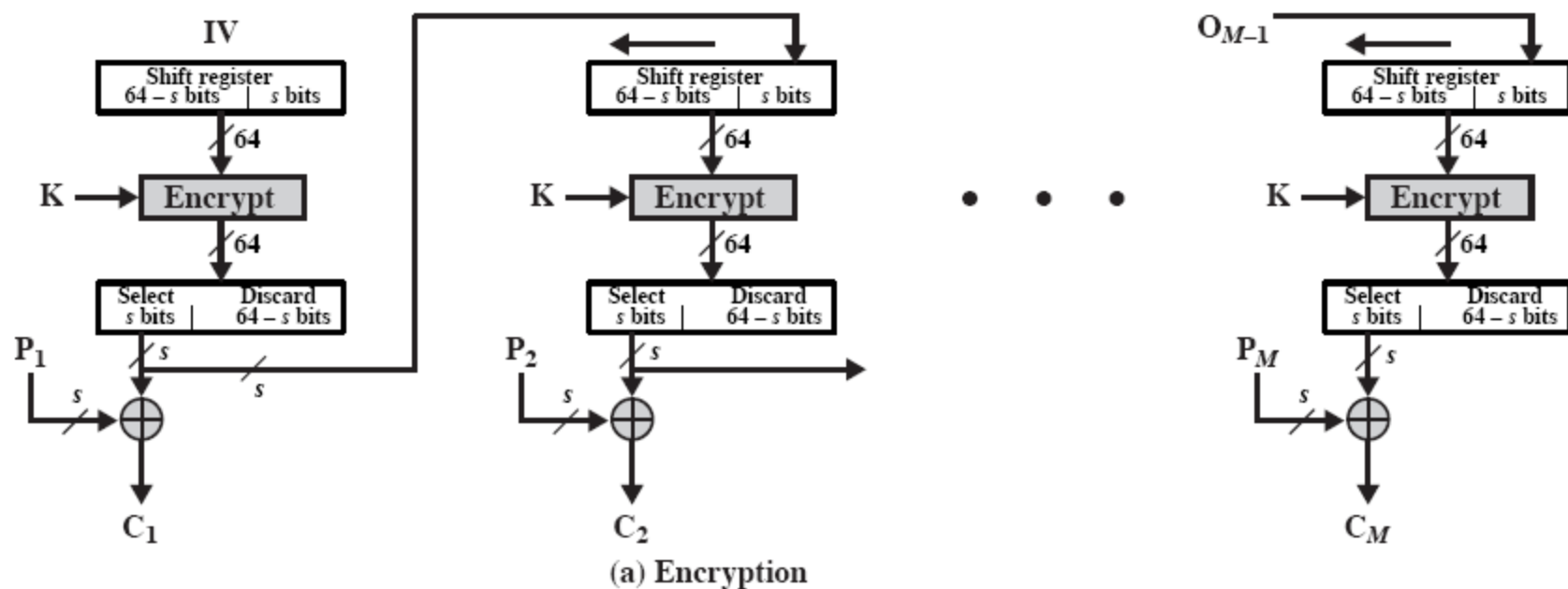


Figure 3.14  $s$ -bit Output Feedback (OFB) Mode

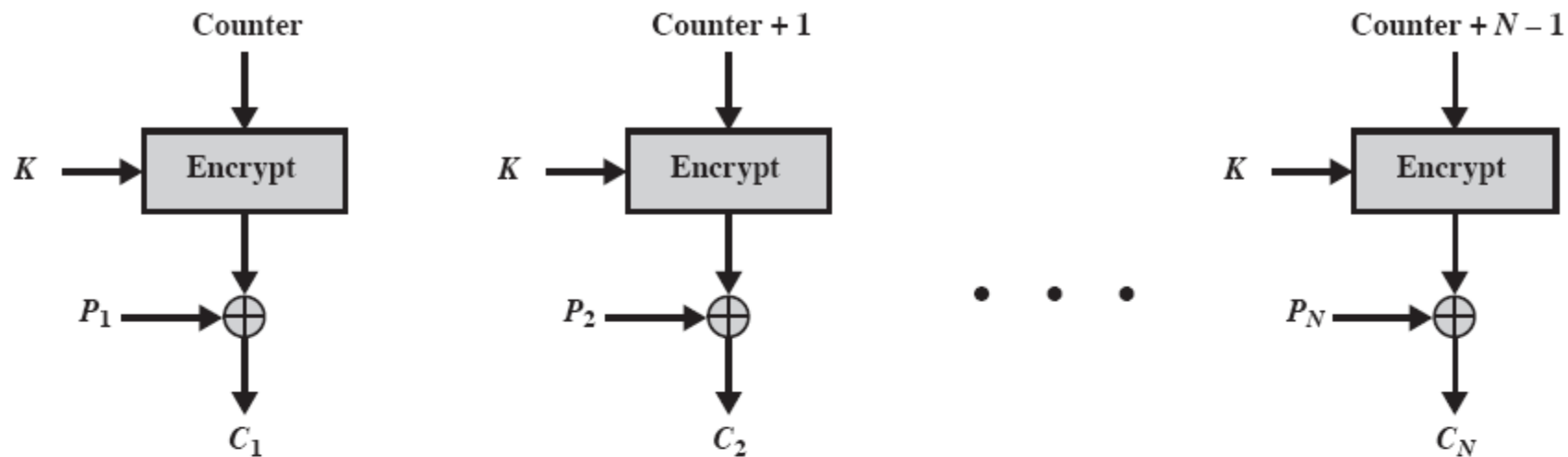
# Remarks on Feedback Mode

## *Advantage*

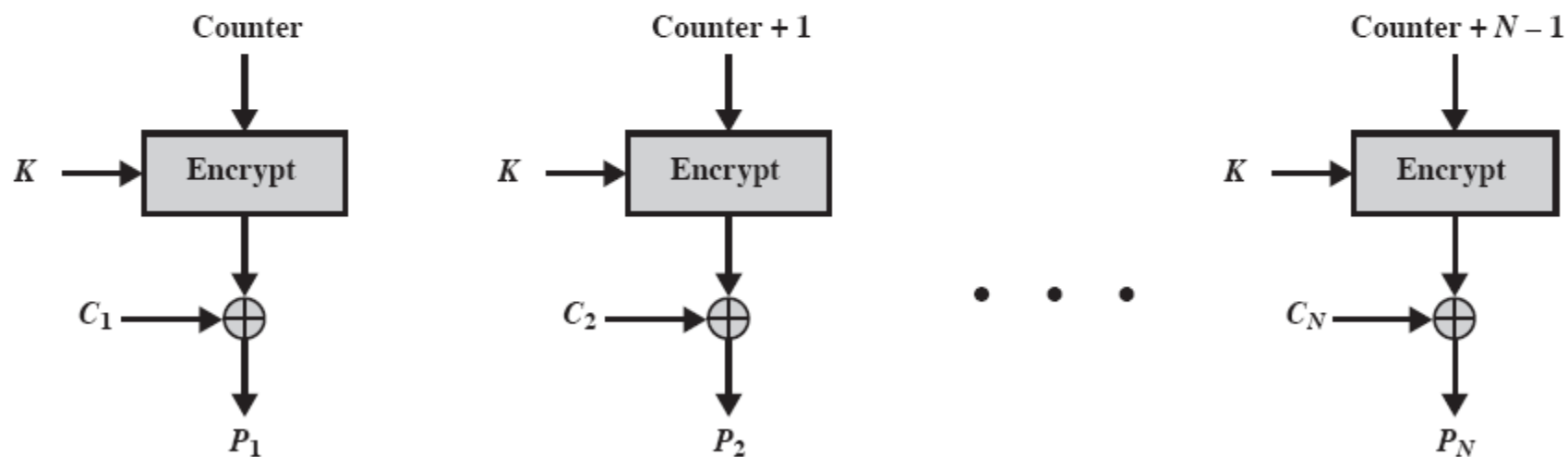
- Free from bit error rate.

## *Disadvantage*

- Vulnerable to a stream modification attack.



(a) Encryption

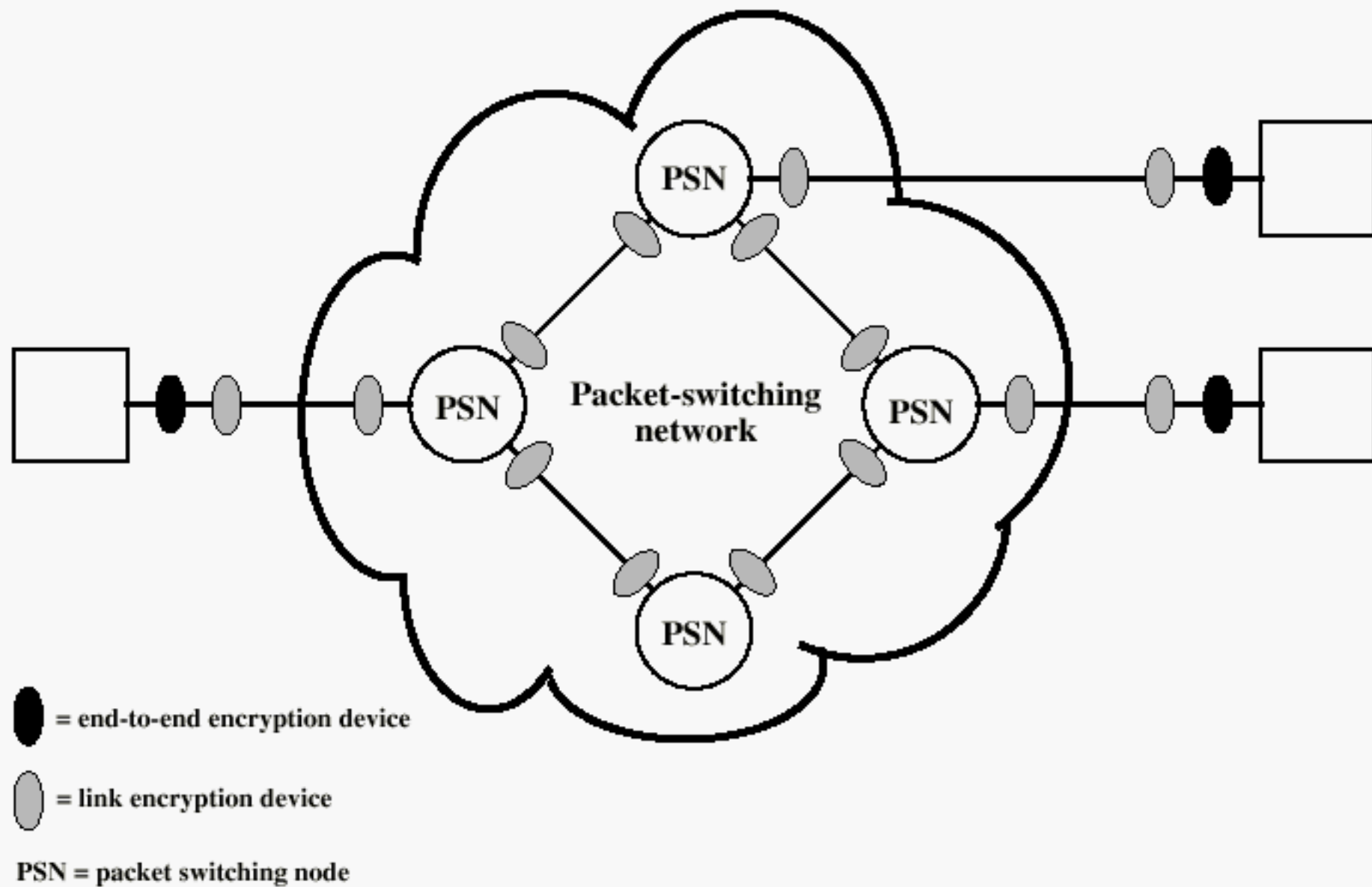


(b) Decryption

Figure 3.15 Counter (CTR) Mode

# Location of Encryption Devices

- **Link encryption:**
  - A lot of encryption devices
  - High level of security
  - Decrypt each packet at every switch
- **End-to-end encryption**
  - The source encrypt and the receiver decrypts
  - Payload encrypted
  - Header in the clear
- **High Security:** Both link and end-to-end encryption are needed (see Figure 2.9)



**Figure 2.9 Encryption Across a Packet-Switching Network**

# Key Distribution

1. A key could be selected by A and physically delivered to B.
2. A third party could select the key and physically deliver it to A and B.
3. If A and B have previously used a key, one party could transmit the new key to the other, encrypted using the old key.
4. If A and B each have an encrypted connection to a third party C, C could deliver a key on the encrypted links to A and B.

# Key Distribution (See Figure 2.10)

- **Session key:**
  - Data encrypted with a one-time session key. At the conclusion of the session the key is destroyed
- **Permanent key:**
  - Used between entities for the purpose of distributing session keys

1. Host sends packet requesting connection
2. Front end buffers packet; asks KDC for session key
3. KDC distributes session key to both front ends
4. Buffered packet transmitted

FEP = front end processor  
KDC = key distribution center

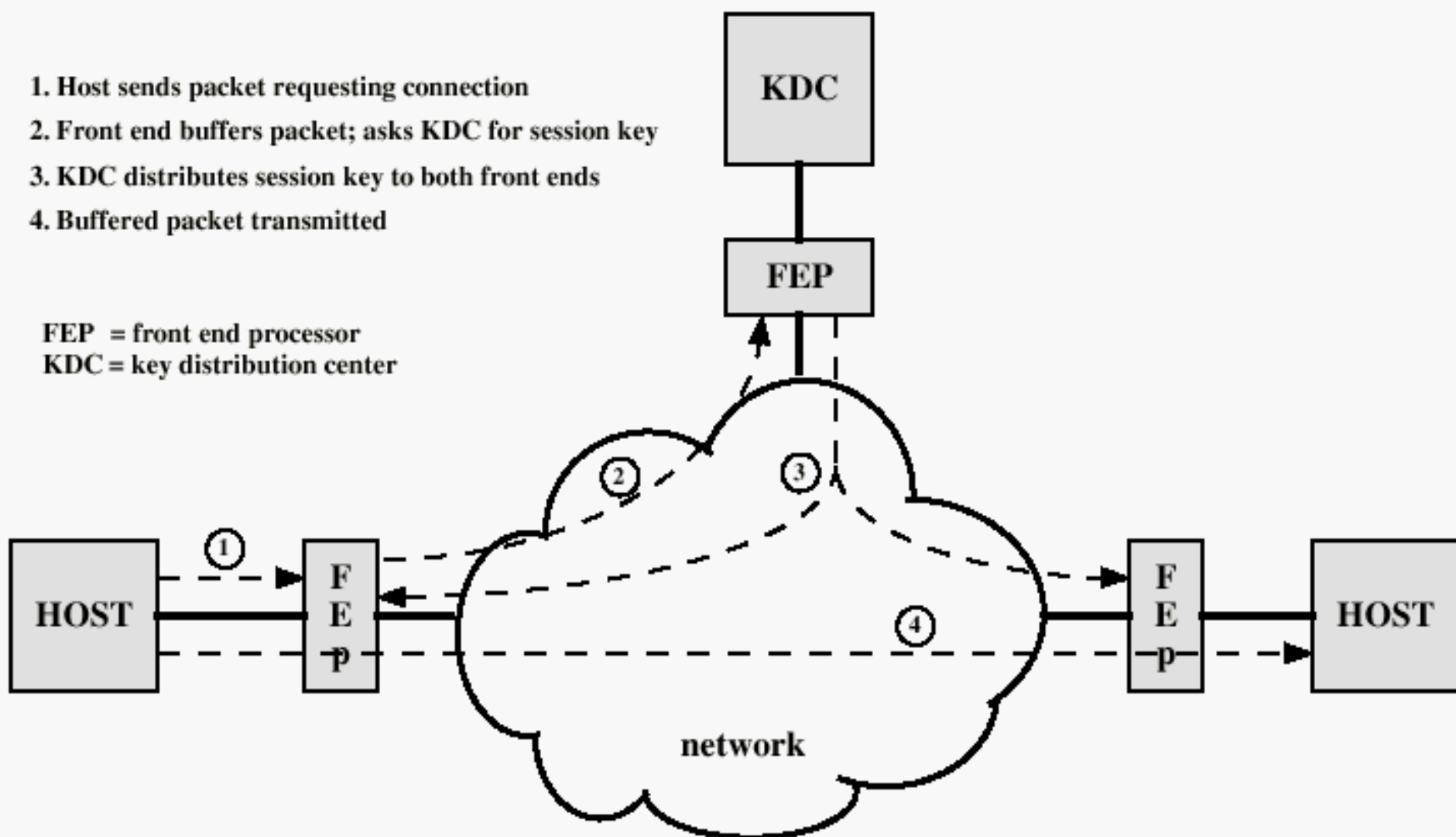


Figure 2.10 Automatic Key Distribution for Connection-Oriented Protocol

# Authentication

- **Requirements** - must be able to verify that:
  1. Message came from apparent source or author,
  2. Contents have not been altered,
  3. Sometimes, it was sent at a certain time or sequence.
- Protection against active attack (falsification of data and transactions)

# Approaches to Message Authentication

## 1. Authentication Using Conventional Encryption

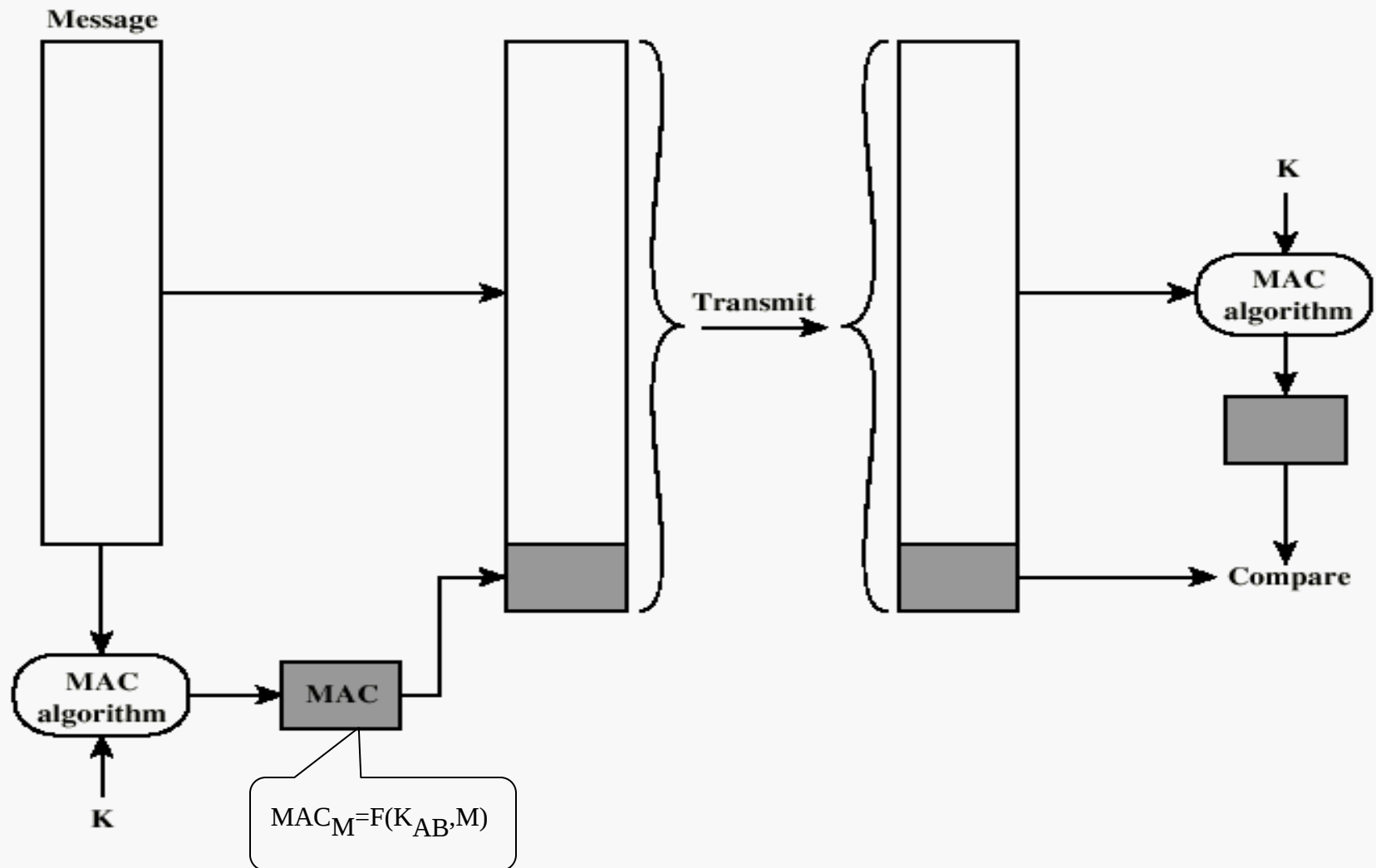
Only the sender and receiver should share a key.

Message with an error-detection code and a sequence no, timestamp.

## 2. Message Authentication without Message Encryption

- -Message Authentication Code
- -One-Way hash function

## 2. Message Authentication without Message Encryption - Message Authentication Code



**Figure 3.1** Message Authentication Using a Message Authentication Code (MAC)

If received code matches the calculated code, then:

- The receiver is assured that the message has not altered.
- The receiver is assured that the message is from the alleged sender.
- If the message includes a sequence number, then the receiver can be assured of the proper sequence, because an attacker cannot successfully alter the sequence number.

## 2. Message Authentication without Message Encryption

- -One-Way hash function

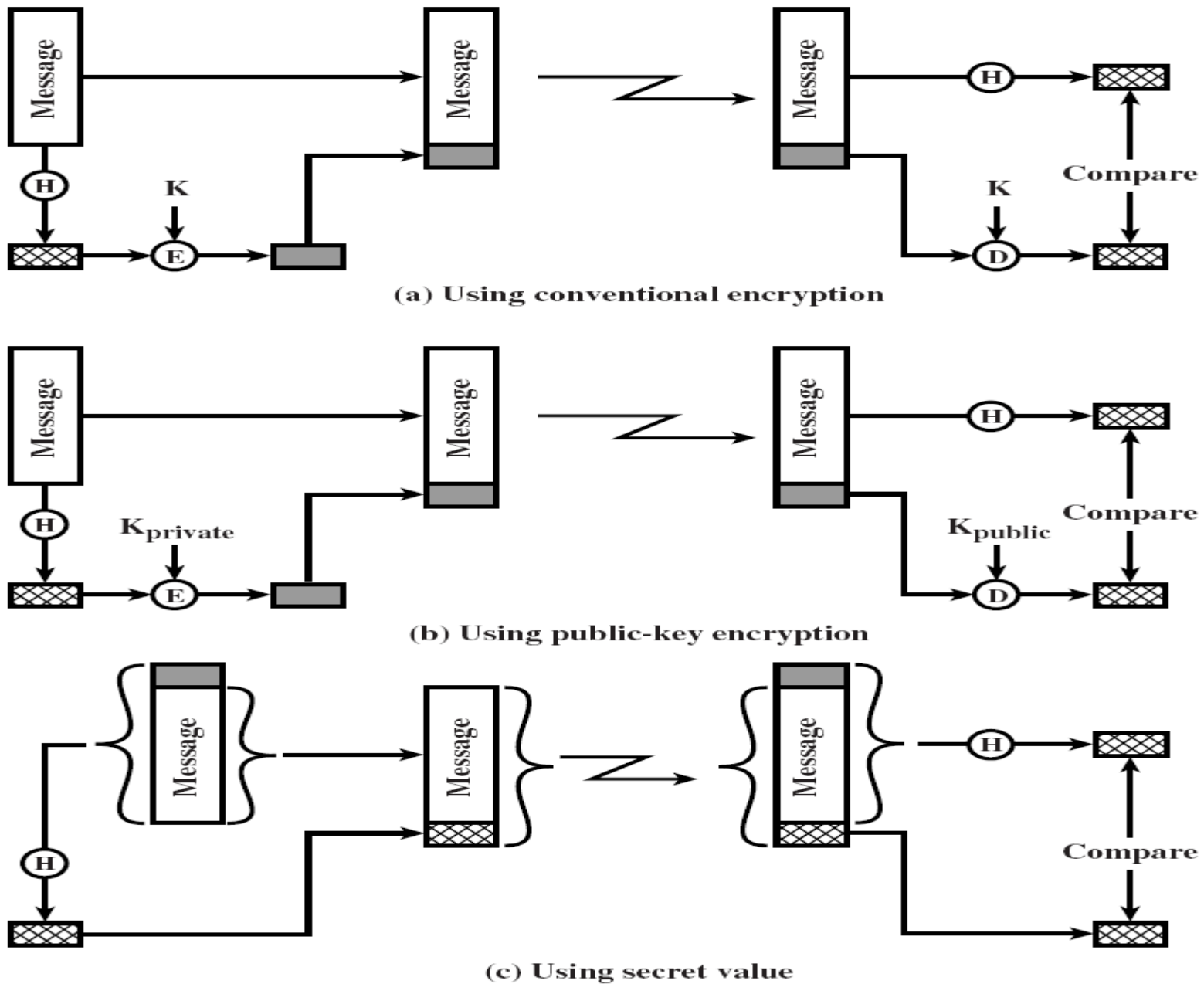


Figure 3.2 Message Authentication Using a One-Way Hash Function

# Secure HASH Functions

Purpose of the HASH function is to produce a "fingerprint."

## Properties of a HASH function $H$ :

1.  $H$  can be applied to a block of data of any size
2.  $H$  produces a fixed length output
3.  $H(x)$  is easy to compute for any given  $x$ .
4. For any given code  $h$ , it is computationally infeasible to find  $x$  such that  $H(x) = h$
5. For any given block  $x$ , it is computationally infeasible to find  $y \neq x$  with  $H(y) = H(x)$ .
6. It is computationally infeasible to find any pair  $(x, y)$  such that  $H(x) = H(y)$

# Simple Hash Function

|           | bit 1    | bit 2    | • • • | bit $n$  |
|-----------|----------|----------|-------|----------|
| block 1   | $b_{11}$ | $b_{21}$ |       | $b_{n1}$ |
| block 2   | $b_{12}$ | $b_{22}$ |       | $b_{n2}$ |
|           | •        | •        | •     | •        |
|           | •        | •        | •     | •        |
|           | •        | •        | •     | •        |
| block $m$ | $b_{1m}$ | $b_{2m}$ |       | $b_{nm}$ |
| hash code | $C_1$    | $C_2$    |       | $C_n$    |

$b_{11} \text{ xor } b_{12} \text{ xor } \dots \text{ xor } b_{1m}$

**Figure 3.3 Simple Hash Function Using Bitwise XOR**

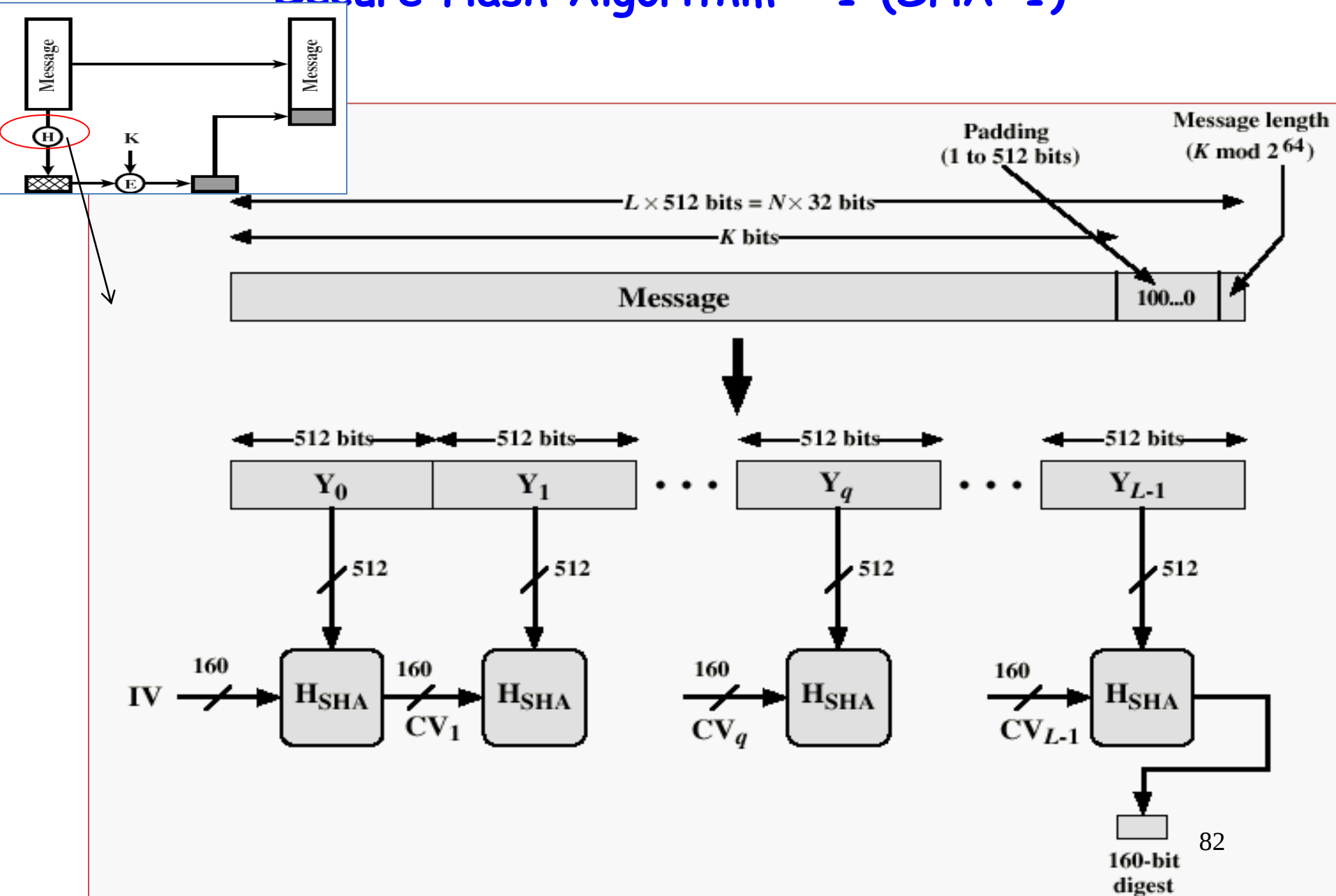
# • SHA-1

- ✓ The algorithm takes as input a message with a maximum length of less than  $2^{64}$  bits and produces as output a 160-bit message digest.
- ✓ The input is processed in 512-bit blocks.

## Steps

1. pad message so its length is 448 mod 512
2. append a 64-bit length value to message
3. initialise 5-word (160-bit) buffer (A,B,C,D,E) to (67452301,efcdab89,98badcfe,10325476,c3d2e1f0)
4. process message in 16-word (512-bit) blocks:
  - expand 16 words into 80 words by mixing & shifting
  - use 4 rounds of 20 bit operations on message block & buffer
  - add output to input to form new buffer value
5. output hash value is the final buffer value

# Message Digest Generation Using Secure Hash Algorithm - 1 (SHA-1)



# SHA-1 Processing of single 512-Bit Block

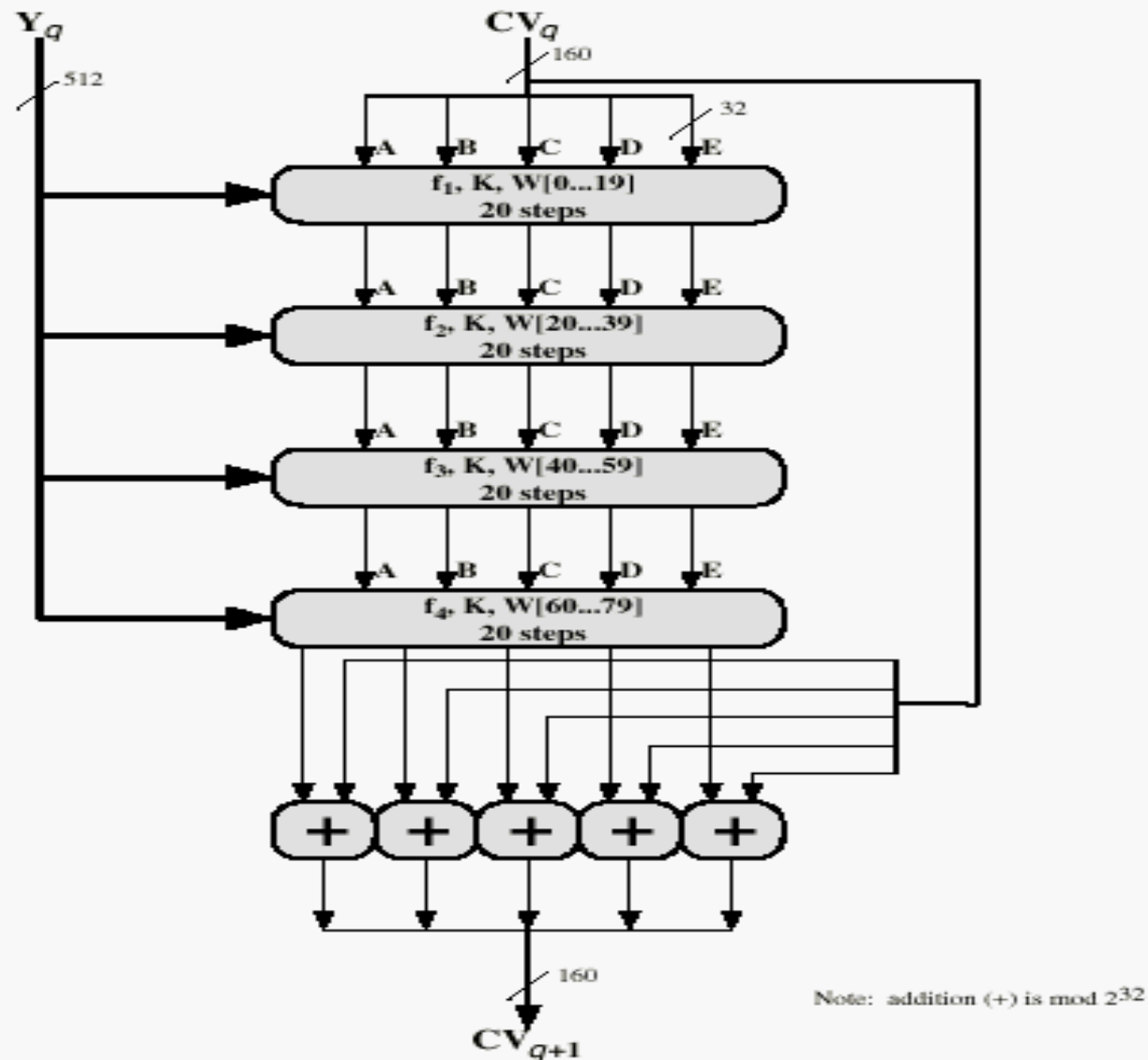
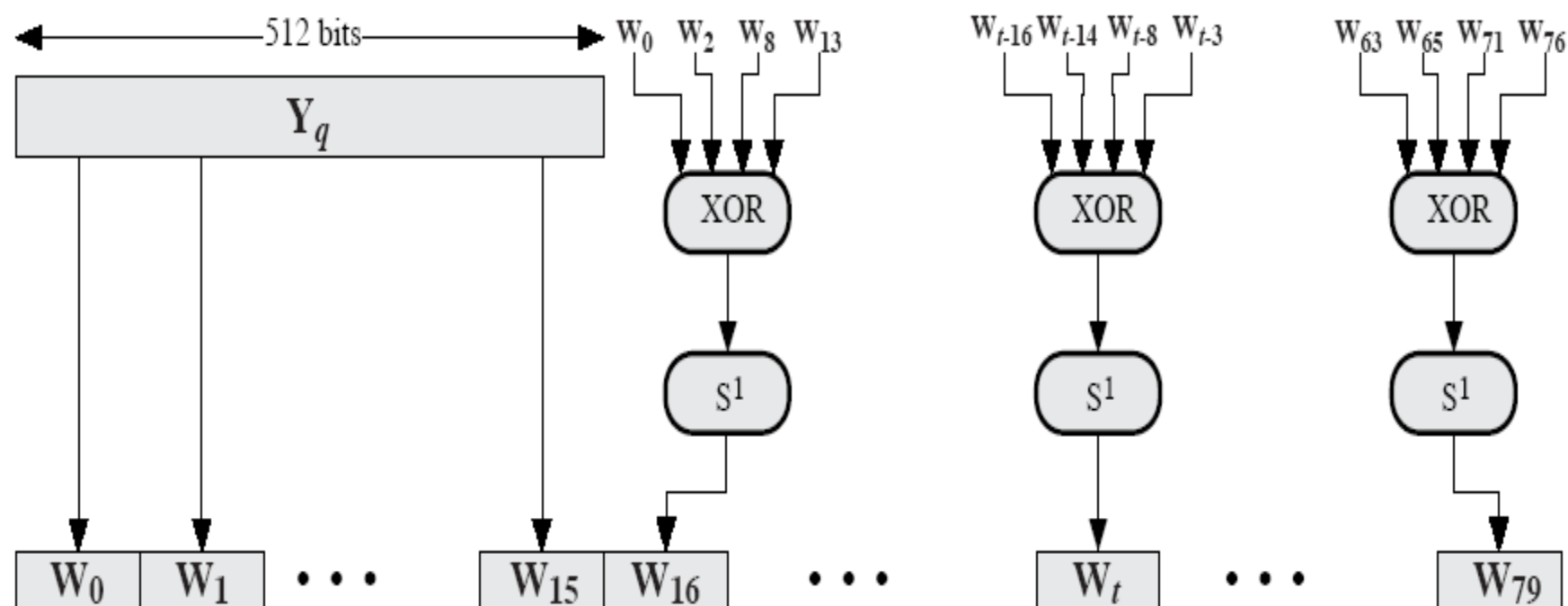
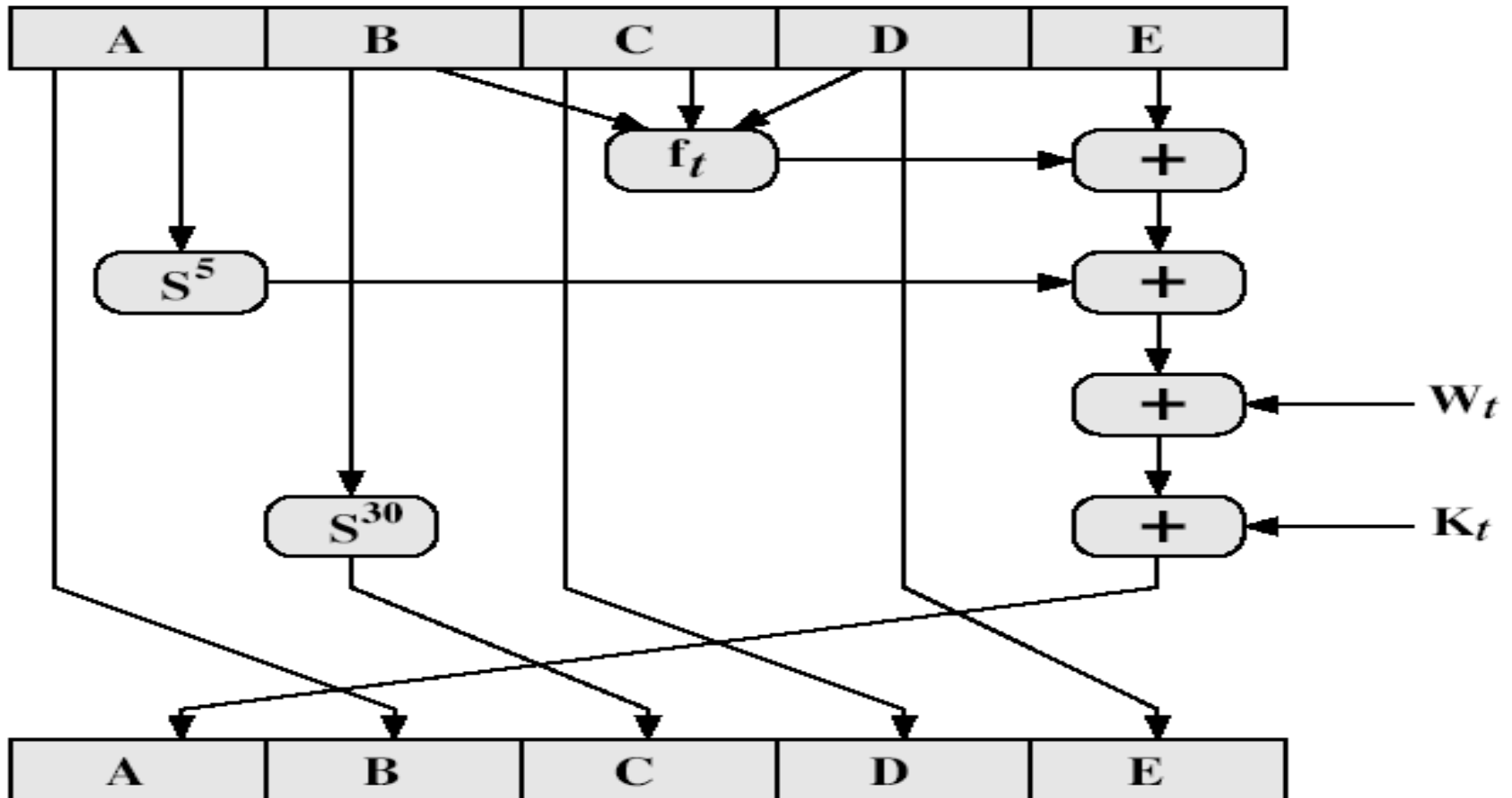


Figure 3.5 SHA-1 Processing of a Single 512-bit Block



**Figure 12.7** Creation of 80-word Input Sequence for SHA-1 Processing of Single Block

# SHA-1 Compression Function



## SHA-1 Compression Function

- each round has 20 steps which replaces the 5 buffer words thus:

$$(A, B, C, D, E) \leftarrow (E + f(t, B, C, D) + S^5(A) + W_t + K_t), A, S^{30}(B), C, D$$

- $a, b, c, d$  refer to the 4 words of the buffer
- $t$  is the step number
- $f(t, B, C, D)$  is nonlinear function for round
- $W_t$  is derived from the message block
- $K_t$  is an additive constant
- $+$  addition modulo  $2^{32}$

# Other Secure HASH functions

Table 3.1 A Comparison of Secure Hash Functions

|                             | MD5                 | SHA-1               | RIPMD-160                   |
|-----------------------------|---------------------|---------------------|-----------------------------|
| Digest length               | 128 bits            | 160 bits            | 160 bits                    |
| Basic unit of processing    | 512 bits            | 512 bits            | 512 bits                    |
| Number of steps             | 64 (4 rounds of 16) | 80 (4 rounds of 20) | 160 (5 paired rounds of 16) |
| Maximum message size        | $\infty$            | $2^{64} - 1$ bits   | $\infty$                    |
| Primitive logical functions | 4                   | 4                   | 5                           |
| Additive constants used     | 64                  | 4                   | 9                           |

# HMAC

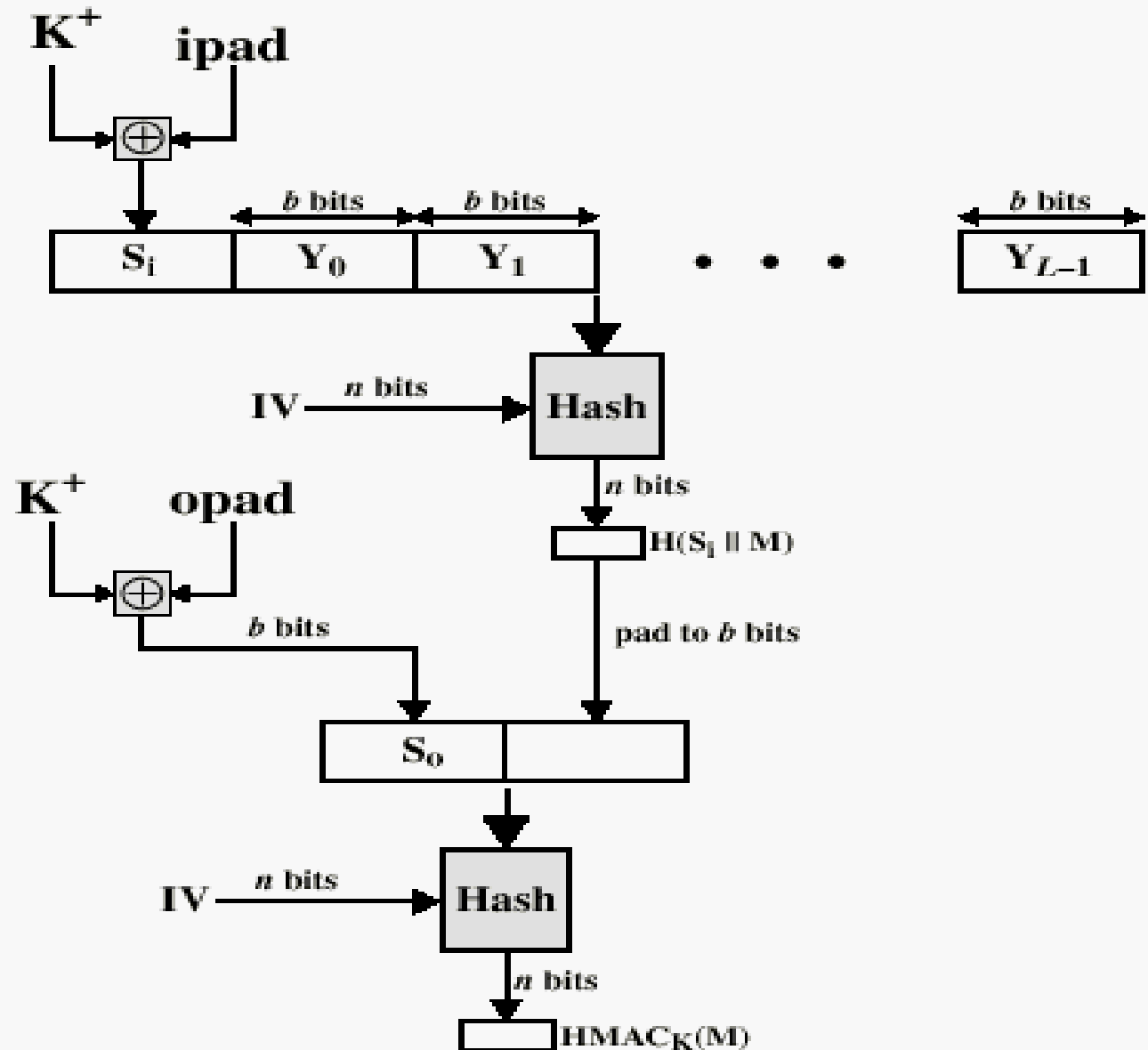
- Use a MAC derived from a cryptographic hash code, such as SHA-1.
- **Motivations:**
  - Cryptographic hash functions executes faster in software than encryption algorithms such as DES
  - Library code for cryptographic hash functions is widely available
  - No export restrictions from the US

A **cryptographic hash function**: **hash function** which takes an input (or 'message') and returns a fixed-size alphanumeric string, which is called the **hash** value (sometimes called a message digest, a digital fingerprint, a digest or a checksum).

# HMAC Design Objectives

- To use without modifications, available hash functions-in particular, hash functions that perform well in software, and for which code is freely and widely available.
- To allow for easy replaceability of the embedded hash functions in case faster or more secure hash functions are found or required.
- To preserve the original performance of the hash functions without incurring a significant degradation.
- To use and handle keys in a simple way.
- To have a well understood cryptographic analysis of the strength of the authentication mechanism based on reasonable assumptions about embedded hash function.

# HMAC Structure



H = embedded hash function (e.g., SHA-1)

IV= initial value input to hash function

M = message input to HMAC (including the padding specified in the embedded hash function)

$Y_i$  = i th block of M,  $0 \leq i \leq (L-1)$

L = number of blocks in M

b = number of bits in a block

n = length of hash code produced by embedded hash function

K = secret key; if  $\text{key} > b$ ; the key is input to hash fun to produce an n-bit key: recommended length is  $\geq n$ .

$K^+$  = K padded with zeros on the left so that the result is b bits in length

ipad = 00110110 (36 in hexadecimal) repeated b/8 times

opad = 01011100 (5C in hexadecimal) repeated b/8 times

Then HMAC can be expressed as follows:

- $$\text{HMAC}_k = H[(K^+ \oplus \text{opad}) \parallel H[(K^+ \oplus \text{ipad}) \parallel M]]$$

- HMAC Algorithm

1. Append zeros to the left end of  $K$  to create a  $b$ -bit string  $K^+$  (e.g., if  $K$  is of length 160 bits and  $b=512$ , then  $K$  will be appended with 44 zero bytes  $0x00$ ).
2. XOR  $K^+$  with  $ipad$  to produce the  $b$ -bit block  $s_i$
3. Append  $M$  to  $s_i$
4. Apply  $H$  to the stream generated in step3
5. XOR  $K^+$  with  $opad$  to produce the  $b$ -bit block  $s_0$
6. Append the hash result from step4 to  $s_0$
7. Apply  $H$  to the stream generated in step6 and output the result.